

Article

A Unified Framework for Street-View Panorama Stitching

Li Li ¹, Jian Yao ^{1,*}, Renping Xie ¹, Menghan Xia ¹ and Wei Zhang ²

¹ School of Remote Sensing and Information Engineering, Wuhan University, Wuhan, Hubei, P.R. China

² School of Control Science and Engineering, Shandong University, Jinan, Shandong, P.R. China

* Correspondence: jian.yao@whu.edu.cn; Tel.: +86-27-68771218; Web: <http://cvrs.whu.edu.cn/>

Version September 7, 2016 submitted to Remote Sens.; Typeset by L^AT_EX using class file mdpi.cls

Abstract: In this paper, we propose a unified framework to generate a pleasant and high-quality street-view panorama by stitching multiple panoramic images captured from the cameras mounted on the mobile platform. Our proposed framework is comprised of four major steps: image warping, color correction, optimal seamline detection and image blending. Since the input images are captured without a precisely common projection center from the scenes with the depth differences with respect to cameras to different extents, such these images cannot be precisely aligned in geometry. So, an efficient image warping method based on the dense optical flow field is proposed to greatly suppress the influence of large geometric misalignment at first. Then, to lessen the influence of photometric inconsistencies caused by the illumination variations and different exposure settings, we propose an efficient color correction algorithm via matching extreme points of histograms to greatly decrease color differences between warped images. After that, the optimal seamlines between adjacent input images are detected via the graph cuts energy minimization framework. At last, the Laplacian pyramid blending algorithm is applied to further eliminate the stitching artifacts along the optimal seamlines. Experimental results on a large set of challenging street-view panoramic images captured from the real world illustrate that the proposed system is capable of creating high-quality panoramas.

Keywords: Panorama Stitching ; Seamline Detection ; Image Warping ; Graph Cuts ; Image Parallax ; Image Blending ; Color Correction

1 Introduction

Nowadays, as the development of street-view panoramas which provide 360° panoramic views along streets in the real world, the demand for high-quality panoramic images gradually becomes bigger. Image stitching is the key technology to produce high-quality panoramic images, which is also an important and classical problem in the field of photogrammetry [1–5], remote sensing [6–9] and computer vision [10–15], which is widely used to merge multiple aligned images into a single wide-angle composite image as seamlessly as possible.

In an ideally static scene in which both the geometric misalignments and the photometric inconsistencies don't exist or are not obviously visible in overlap regions, the stitched or mosaicked image looks perfect only when the geometric distance criterion is used. However, as we know, most of street-view panoramic images are captured by the panoramic camera mounted on the mobile platform. Generally, the panoramic camera is comprised of multiple wide-angle or fish-eye cameras whose projection centers are slightly different. Therefore, those images cannot be precisely aligned in geometry, namely, there exist the geometric deviations for corresponding pixels from different images to different extents. In addition, there also exist photometric inconsistencies to different extents in

34 overlap regions between adjacent images due to illumination variations and/or different exposure
35 setting. This paper focuses on creating a visually pleasant street-view panorama by stitching or
36 mosaicking the street-view panoramic images among which there may exist the severe geometric
37 misalignments and the strong photometric inconsistencies.

38 One traditional and efficient way to eliminate the stitching artifacts caused by the large geometric
39 misalignments existed in the input aligned panoramic images is to detect the optimal seamlines
40 which avoid crossing majority of visually obvious objects and most of overlap regions with low
41 image similarity and large object dislocation. The optimal seamline detection methods search for
42 the seamlines in overlap regions between images where their intensity or gradient differences are not
43 significant. Based on the optimally detected seamlines, multiple aligned images can be mosaicked
44 into a single composite image in which the obvious image parallax caused by image misalignments
45 can be magnificently concealed. Many methods [2–6,16–19] regarded the optimal seamline detection
46 as an energy optimization problem and solved it by minimizing a specially designed energy function
47 defined to represent the difference between the original images along the seamlines. For these
48 methods, the key ideas concentrate on how to define the effective energy functions and how to
49 guarantee the optimality of the solution. The energy functions are often defined by considering color,
50 gradient and texture, and are optimized via different optimization algorithms, e.g., snake model [20],
51 Dijkstra's algorithm [21], dynamic programming [22], and graph cuts [23]. Nowadays, the optimal
52 seamline detected by many algorithms can avoid crossing the regions with low image similarity and
53 high object dislocation. In our previous work presented in [19], we proposed an efficient optimal
54 seamline detection algorithm for mosaicking aerial and panoramic images based on the graph cuts
55 energy minimization framework. In this paper, we will apply this algorithm to detect the optimal
56 seamlines.

57 However, when the geometric misalignments are very large, the stitching artifacts maybe
58 cannot be completely avoided even though the optimal seamlines are detected, especially for
59 street-view panoramic images among which there always exist geometric misalignments at different
60 extents due to that those images were captured from the scenes with large depth differences by
61 the panoramic camera comprised of multiple wide-angle or fish-eye cameras without a precisely
62 common projection center, which means that the geometric misalignments are different at different
63 positions. Therefore, the large geometric misalignments existed in the input aligned panoramic
64 images should be eliminated as much as possible before finding the optimal seamlines. In this
65 paper, we creatively propose an image warping algorithm based on the optical flow field to reduce
66 the geometric misalignments between input panoramic images. Image warping is a transformation
67 which maps all positions in one image plane to the corresponding ones in another plane [24], which
68 has been popularly applied in many fields of computer vision, such as image morphing [25,26],
69 image retargeting [27,28] and image mosaicking [29,30]. The key technique of image warping is to
70 find the appropriate transformation functions based on the control conditions and then eliminate the
71 distortions between input images. One famous image warping algorithm worked based on thin-plate
72 splines [31] that attempted to minimize the amount of bending in the deformation. They used the
73 radial basis functions with thin-plate splines to find a space deformation defined by control points.
74 However, the local non-uniform scaling and shearing possibly occurred in the deformed images. [32]
75 firstly introduced the concept of as-rigid-as-possible transformations, which have the property that
76 both local scaling and shearing are very slight. To produce as-rigid-as-possible deformations, [33]
77 proposed a point-based image deformation technique, which firstly triangulated the input image, and
78 then geometrically minimized the distortion associated with each triangle. However, this algorithm
79 needs to triangulate the input image at first, and the results are maybe not smooth across triangle
80 boundaries. [34] provided an image deformation method based on Moving Least Squares [35]
81 using various classes of linear functions including affine, similarity and rigid transformations. It
82 first found the deformation functions based on the control points or the line segments, and then
83 applied the deformation functions onto each grid instead of each pixel to reduce the transformation

84 time. At last, it filled the resulting quads using the bilinear interpolation. [36] proposed an image
85 warping algorithm based on radial basis functions, which formulated the image warping problem
86 as the scattered data interpolation problem, and used the radial basis functions to construct the
87 interpolation. It aimed to identify the best radial basis functions for image warping. Our used image
88 warping method is similar to this algorithm, but we used the Multilevel B-Splines Approximation
89 (MBA) [37] to solve the scattered data interpolation problem. Recently, the b-spline approximation
90 technique has been widely used for image registration [38,39], image morphing, image warping,
91 curve/surface fitting and geometric modeling.

92 In addition, due to the differences of both the image capturing viewpoints and the camera
93 exposure settings, there are large differences of color and brightness between the warped panoramic
94 images. The large color differences between those images also can cause the stitching artifacts in the
95 last stitched or mosaicked panorama. Also, the large color differences maybe affect the quality of the
96 seamlines. So, we also need to suppress the color differences between warped images before we apply
97 the optimal seamline detection. Generally, the color correction approaches can be divided into two
98 broad categories according to [40]: parametric and non-parametric. Panoramic approaches assume
99 that the color relationship between images can be described by a certain model. Few noteworthy
100 parametric approaches are described here. [41] proposed a simple linear model to transform the
101 color of the source image to the target image. The transformation matrix was estimated by using the
102 histogram mapping over the overlap regions. [12] applied the gain compensation (i.e., the diagonal
103 model) to reduce color differences between input images. They computed all gains by minimizing an
104 error function, which is the sum of gain normalised intensity errors for all overlapping pixels. [42]
105 also employed the diagonal model for the color and luminance compensation where the correction
106 coefficients were computed as the ratio of sum of pixel values in the overlap regions. As stated in [43],
107 the linear transformation models can provide a simple yet effective way to transform colors, but they
108 have clear limitations in explaining the complicated nonlinear transformations in the the imaging
109 process. Non-parametric approaches can handle this problem well. Non-parametric approaches
110 don't follow any particular model for the color mapping, and most of them use some form of a
111 look-up table to record the mapping of the full range of color levels. As stated in [40], parametric
112 approaches are more effective in extending the color in non-overlap regions without generating gain
113 artifacts, while non-parametric approaches can provide better color matching results. [44] proposed
114 to use the joint histogram of correspondences matched using the SIFT features [45] to correct the color
115 differences. The color mapping function was estimated by using an energy minimization scheme.
116 [46] proposed a color correction approach by using the cumulative color histogram. This method
117 used the cumulative histogram-based mapping to automatically adapt the color of all source images
118 to the reference image. [43] presented a nonlinear and nonparametric color transfer framework that
119 operates in a 3D color space. Based on some control corresponding colors in a given image pair,
120 this method used the probabilistic moving least squares to interpolate the transformation functions
121 for each color. We correct the color differences between two images based on the matched extreme
122 points which are extracted from the histograms over the overlap regions. Both the Probability Density
123 Functions (PDFs) and Cumulative Distribution Functions (CDFs) are used to find the reliably matched
124 extreme points. To reduce the gain artifacts in non-overlap regions, we propose to apply the alpha
125 correction method to smooth the transition from non-overlap regions to overlap ones.

126 Although we propose efficient approaches to correct the color differences and detect the optimal
127 seamlines between warped panoramic images, there maybe also exist some color transitions along
128 the seamlines due to that the color differences cannot be eliminated completely. In order to further
129 conceal these artifacts, the image blending techniques can be further applied along the seamlines.
130 In the last several decades, many image blending algorithms have been proposed to smooth the
131 color differences along the seamlines, such as feathering [47], alpha blending [48], Laplacian pyramid
132 blending [49], poisson blending [50] and gradient domain image blending approach [51]. In this



Figure 1. Our proposed unified framework for the street-view panorama stitching system.

133 paper, we simply applied the Laplacian pyramid blending algorithm [49] to eliminate the stitching
 134 artifacts and generate the last pleasant panorama.

135 In this paper, we propose a unified framework for our developed street-view panorama stitching
 136 system, as described in Figure 1. First, multiple original images, which were captured from a
 137 single panoramic camera comprised of multiple wide-angle or fish-eye cameras (usually digital SLR
 138 cameras) without a precisely common projection center, are fed into our stitching system as the input.
 139 Therefore, we will align these input images into a common spherical coordinate system based on the
 140 found feature correspondences using the existing open-source library. After that, our proposed image
 141 warping method based on the dense optical flow field approximately interpolated from the sparse
 142 feature matches, which is detailed described in Section 2, is used to greatly reduce the geometric
 143 misalignments. Then, an automatic contrast adjustment and an efficient histogram-matching-based
 144 color correction approach presented in Section 3 are used to reduce the color differences. Finally,
 145 we adopt an efficient seamline detection approach based on the graph cuts energy minimization
 146 framework to find the optimal seamlines between two overlapped images followed by applying
 147 the image blending to eliminate the color transitions along the seamlines. By our proposed unified
 148 panorama stitching framework, our system can generate a pleasant street-view panorama as seamless
 149 as possible by stitching multiple panoramic images from the cameras mounted on the mobile
 150 platform. Experimental results on challenging street-view panoramic images are reported in Section 5
 151 followed by the conclusions drawn in Section 6.

152 2 Image Warping

153 In our developed street-view panorama stitching system, we first check whether all input images
 154 are geometrically aligned into a common spherical coordinate system. If not, we will align them by

155 using the open-source library *PanoTools*¹, which is also served as the underlying core engine for
 156 many image stitching softwares, such as *PTGui*² and *Hugin*³. However, there always exist large
 157 geometric misalignments between these aligned images at different extents because those images
 158 were captured from the scenes of large depth differences by a single panoramic camera comprised
 159 of multiple wide-angle or fish-eye cameras without a precisely common projection center. Those
 160 geometric misalignments are so large that the stitching artifacts cannot be avoided completely even
 161 though the optimal seamlines are detected out for the use of the image stitching. To ensure the
 162 high-quality of the last stitched panorama, we propose to apply the image warping technique to
 163 eliminate those large geometric misalignments as far as possible. To describe our proposed image
 164 warping algorithm more clearly, we first consider a simple case of two aligned images \mathbf{I} and \mathbf{I}' with
 165 an overlap. The process of our proposed image warping algorithm is described as follows. Firstly,
 166 the corresponding points between two images are found as the control points of image warping, and
 167 the sparse optical flows are calculated for those control points. Secondly, the Multilevel B-Splines
 168 Approximation (MBA) algorithm [37] is used to approximately interpolate the dense optical flows
 169 for all integral pixels in the warped image with respective to the original one from the sparse optical
 170 flows. Lastly, we warp the input two images based on the dense optical flows and thus the geometric
 171 misalignments can be greatly lessened. For the case of multiple images to be stitched to the last
 172 panorama, a simple strategy is proposed to first handle the horizontal images and then deal with the
 173 vertical ones.

174 2.1 Feature Point Matching

175 To warp two images with large geometric misalignments, we need to find the control points
 176 at first. The quality of the warped image mainly depends on the accuracy and densities of control
 177 points. In this paper, we apply the feature matching algorithm to robustly find the sparse matching
 178 points, namely the control points. The main ideal for feature matching is to first extract local invariant
 179 features independently from two images and then characterize them by invariant descriptors. The
 180 distance between two descriptor vectors is used to identify candidate matches. However, the
 181 nearest neighbors is not always the best match due to occlusion and deformation derived from
 182 large viewpoint changes and repeated structures in the scenes. Generally, the epipolar geometrical
 183 constraint works well to filter the outliers, but it is not available for the panoramic images aligned in
 184 advance. Thus, we need to apply another strategy to filter the outliers. [52] proposed that the motion
 185 of one match would be consistent with those of neighbors, and the experimental results presented
 186 in [52] sufficiently show that this strategy is simple but effective. Inspired by this idea, we propose a
 187 new feature matching algorithm for panoramic images. The major steps of the proposed algorithm
 188 include initial matching and outlier detection, which are summarized in Algorithm 1. An example
 189 of finding point correspondences between two panoramic images with an overlap is illustrated in
 190 Figure 2.

191 2.1.1 Initial Matching

192 Given two adjacent images \mathbf{I} and \mathbf{I}' with an overlap, the local invariant features are extracted and
 193 described by the SURF algorithm [53]. Let $\mathbf{f} = (\mathbf{x}, \mathbf{d})$ be a feature point where $\mathbf{x} = (x, y)^\top$ denotes
 194 the 2D coordinate of this feature point and \mathbf{d} represents its corresponding invariant descriptor vector,
 195 and $\mathcal{F} = \{\mathbf{f}_i | \mathbf{f}_i = (\mathbf{x}_i, \mathbf{d}_i)\}_{i=1}^M$ and $\mathcal{F}' = \{\mathbf{f}'_j | \mathbf{f}'_j = (\mathbf{x}'_j, \mathbf{d}'_j)\}_{j=1}^N$ be the feature point sets extracted from \mathbf{I}
 196 and \mathbf{I}' , respectively, where M and N denote the numbers of the feature points extracted from \mathbf{I} and \mathbf{I}' ,

¹ Available at <http://www.panoramatools.com/>

² Available at <http://www.ptgui.com/>

³ Available at <http://hugin.sourceforge.net/>

Algorithm 1 The proposed feature point matching algorithm.

1. *Initial Matching*

- (a) Extract and describe two sets of local invariant features from two overlapped images \mathbf{I} and \mathbf{I}' by using the SURF algorithm, respectively;
- (b) Find the initial point matches $\mathcal{M}_{\text{initial}}$ between \mathbf{I} and \mathbf{I}' according to the conditions listed in Section 2.1.1.

2. *Outlier Detection*

- (a) Set the value of λ used in Eq. (3) as λ_{\max} ;
 - (b) Find the neighboring inlier matches $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$ for each match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle \in \mathcal{M}_{\text{initial}}$, and then calculate the mean motion $\boldsymbol{\mu}(\mathbf{f}_p)$ and the standard deviation $\boldsymbol{\sigma}(\mathbf{f}_p)$ of all matches in $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$;
 - (c) Sort all matches in $\mathcal{M}_{\text{initial}}$ in the decreasing order according to their costs defined in Eq. (4), and only check whether the top N_t matches are inliers or outliers in each iteration;
 - (d) Iterate the steps (b)-(c) until the maximum number of iterations is reached or no more outliers can be found in the current iteration.;
 - (e) Decrease the value of λ with the step λ_{step} and iterate the steps (b)-(d) until the smallest value λ_{\min} is reached.
-

197 respectively. Generally, for one feature point \mathbf{f}_p in \mathcal{F} , the feature point \mathbf{f}'_q with the nearest Euclidean
 198 distance $d(\mathbf{f}_p, \mathbf{f}'_q) = \min_{\mathbf{f}'_j \in \mathcal{F}'} \|\mathbf{d}_p - \mathbf{d}'_j\|$ which is not larger than a predefined threshold T_d can be regarded
 199 as the corresponding matching point of \mathbf{f}_p . However, this simple strategy has some drawbacks in
 200 the context of feature matching. This mainly because that the distance values between different
 201 corresponding pairs may vary in a relatively large range, so any permissive distance threshold T_d
 202 can not avoid the appearance of high rate outliers when covers most of the good correspondences.
 203 Thus, we propose to modify the matching strategy as follows. In this paper, we accept two feature
 204 points \mathbf{f}_p and \mathbf{f}'_q as a potential match only when they satisfy the following conditions:

- 205 • The feature points $\mathbf{f}_p \in \mathcal{F}$ and $\mathbf{f}'_q \in \mathcal{F}'$ are the nearest neighbors of each other. Namely, for the
 206 feature point \mathbf{f}_p , \mathbf{f}'_q is its nearest neighbor in \mathcal{F}' . At the same time, for the feature point \mathbf{f}'_q , \mathbf{f}_p is
 207 its nearest neighbor in \mathcal{F} .
- 208 • The Euclidean descriptor vector distance $d(\mathbf{f}_p, \mathbf{f}'_q)$ between two feature points \mathbf{f}_p and \mathbf{f}'_q is not
 209 larger than T_d , i.e., $d(\mathbf{f}_p, \mathbf{f}'_q) = \|\mathbf{d}_p - \mathbf{d}'_q\| \leq T_d$.
- 210 • We represent the nearest distance between \mathbf{f}_p and \mathcal{F}' as $d_1(\mathbf{f}_p, \mathcal{F}') = d(\mathbf{f}_p, \mathbf{f}'_q) = \min_{\mathbf{f}'_j \in \mathcal{F}'} \|\mathbf{d}_p -$
 211 $\mathbf{d}'_j\|$ and the next distance as $d_2(\mathbf{f}_p, \mathcal{F}') = \min_{\mathbf{f}'_j \in \mathcal{F}', \mathbf{f}'_j \neq \mathbf{f}'_q} \|\mathbf{d}_p - \mathbf{d}'_j\|$, respectively. The distance ratio
 212 $r(\mathbf{f}_p, \mathcal{F}') = d_1(\mathbf{f}_p, \mathcal{F}') / d_2(\mathbf{f}_p, \mathcal{F}')$ should be smaller than the predefined threshold T_r . Similarly,
 213 for the feature point \mathbf{f}'_q , the distance ratio $r(\mathbf{f}'_q, \mathcal{F}) = d_1(\mathbf{f}'_q, \mathcal{F}) / d_2(\mathbf{f}'_q, \mathcal{F})$ should be smaller than
 214 T_r too.

215 By this matching strategy, we obtain a set of initial matches denoted as $\mathcal{M}_{\text{initial}} = \{\langle \mathbf{f}_p, \mathbf{f}'_q \rangle | \mathbf{f}_p \in$
 216 $\mathcal{F}, \mathbf{f}'_q \in \mathcal{F}'\}$.

217 **2.1.2 Outlier Detection**

218 After initial matching, there maybe still exist a few outliers in $\mathcal{M}_{\text{initial}}$. Of course, we need to
 219 filter out those outliers. The widely used constraint of the epipolar geometric constraint cannot be
 220 efficiently used in panoramic images, especially when the panoramic images have been aligned into
 221 a common spherical coordinate system in advance. According to the assumption proposed by [52]
 222 that the matches in a small neighborhood tend to have the consistent location changes (i.e., motions).
 223 In this paper, we also apply this assumption to identify the outliers.

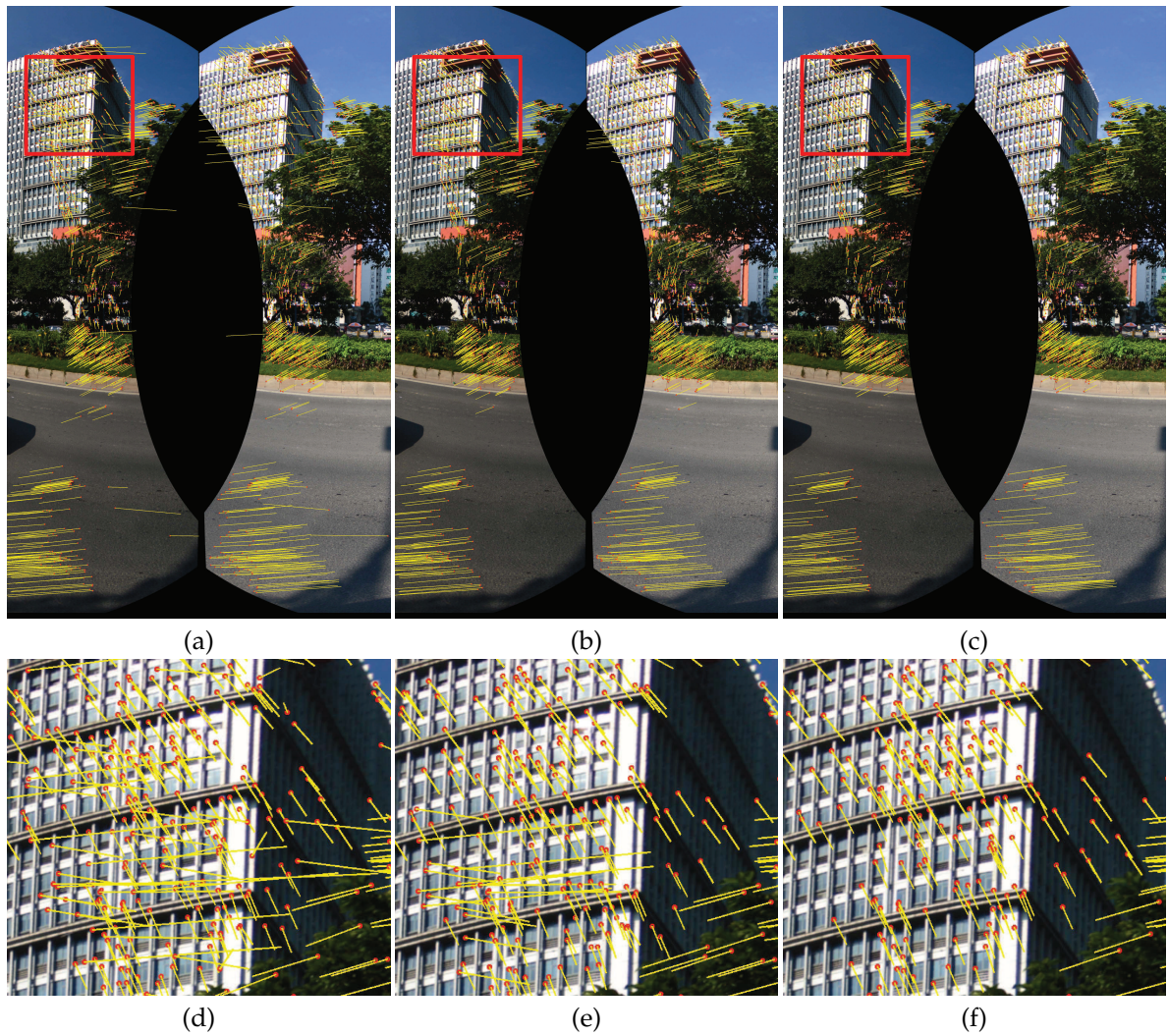


Figure 2. An illustrative example for feature point matching between two aligned panoramic images: (a) the point correspondences produced by initial matching; (b)-(c) the filtered point correspondences after the first iteration ($\lambda = 6$) and the last one ($\lambda = 3$) of outlier detection, respectively. The local detailed regions of (a)-(c) are presented in (d)-(f), respectively. The red circles denote the positions of the matched points in the current image points and the yellow lines represent the optical flows (i.e., motions) of the matched points in the current image with respect to another image.

Given a match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle$, the motions from \mathbf{f}_p to \mathbf{f}'_q along the horizontal direction and the vertical one are calculated, respectively, as follows:

$$\begin{cases} m_p^{(x)} = x'_q - x_p, \\ m_p^{(y)} = y'_q - y_p, \end{cases} \quad (1)$$

where $\mathbf{f}_p = (x_p, y_p)^\top$ and $\mathbf{f}'_q = (x'_q, y'_q)^\top$. Thus, the magnitude value of the motion vector $(m_p^{(x)}, m_p^{(y)})^\top$ can be calculated as:

$$m_p^{(x,y)} = \sqrt{(m_p^{(x)})^2 + (m_p^{(y)})^2}. \quad (2)$$

224 Here, we use $\mathbf{m}(\mathbf{f}_p) = (m_p^{(x)}, m_p^{(y)}, m_p^{(x,y)})^\top$ to represent all the three motion components of the match
 225 $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle$.

At first, we assign the labels of all matches as *Inlier*, namely, for each match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle \in \mathcal{M}_{\text{initial}}$, the label $\mathcal{L}(\langle \mathbf{f}_p, \mathbf{f}'_q \rangle) = \text{Inlier}$, and then we iteratively find the outliers. For each match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle \in \mathcal{M}_{\text{initial}}$, we find K_n ($K_n = 60$ was used in this paper) neighboring match points of \mathbf{f}_p from \mathcal{F} denoted as the set $\mathcal{N}(\mathbf{f}_p)$. Then we collect all matches whose labels are *Inlier* from $\mathcal{N}(\mathbf{f}_p)$ as a new set $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$. If the number of inliers in $\mathcal{N}(\mathbf{f}_p)$, namely, the size of $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$, is less than K_i ($K_i = 10$ was used in this paper), we directly label this match as an *Outlier*, namely, $\mathcal{L}(\langle \mathbf{f}_p, \mathbf{f}'_q \rangle) = \text{Outlier}$, otherwise, we determine whether this match is an inlier by checking whether it has the consistent motion with its neighbors $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$. For each match $\langle \mathbf{f}_m, \mathbf{f}'_n \rangle \in \mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$, the motion $\mathbf{m}(\mathbf{f}_m)$ from \mathbf{f}_m to \mathbf{f}'_n can be calculated according to both Eq. (1) and Eq. (2). Then, the mean motion $\boldsymbol{\mu}(\mathbf{f}_p) = (\mu_p^{(x)}, \mu_p^{(y)}, \mu_p^{(x,y)})^\top$ and the standard deviation of all the motions $\boldsymbol{\sigma}(\mathbf{f}_p) = (\sigma_k^{(x)}, \sigma_k^{(y)}, \sigma_k^{(x,y)})^\top$ of all match points in $\mathcal{N}_{\text{inlier}}(\mathbf{f}_p)$ can be determined easily. According to the following measurement proposed by [52], the label of the match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle$ can be determined as follows:

$$\mathcal{L}(\langle \mathbf{f}_p, \mathbf{f}'_q \rangle) = \begin{cases} \text{Inlier}, & \text{dist}(\mathbf{m}(\mathbf{f}_p), \boldsymbol{\mu}(\mathbf{f}_p)) \leq \lambda \times \boldsymbol{\sigma}(\mathbf{f}_p), \\ \text{Outlier}, & \text{Otherwise,} \end{cases} \quad (3)$$

226 where $\text{dist}(\mathbf{m}(\mathbf{f}_p), \boldsymbol{\mu}(\mathbf{f}_p)) = |\mathbf{m}(\mathbf{f}_p) - \boldsymbol{\mu}(\mathbf{f}_p)|$ denotes the absolute distances in three components
 227 between the motion $\mathbf{m}(\mathbf{f}_p)$ of the match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle$ and the mean motion $\boldsymbol{\mu}(\mathbf{f}_p)$ of its neighbor matches,
 228 and λ is a predefined parameter. However, this measurement has two following drawbacks. To
 229 overcome these two drawbacks, we propose the corresponding strategies.

230 One drawback is that the inliers around the outliers may also be labeled as *Outlier*. As shown in
 231 Figure 3, apparently, the black point with the inconsistent motion with its neighbors is the outlier, we
 232 can remove it easily according to the measurement defined in Eq. (3). However, due to the existence
 233 of this outlier, the inliers (marked in red points) around it maybe also have large deviations with
 234 respective to the corresponding mean motions. So, those inliers may also be regarded as outliers. But,
 235 if we remove the black point as an outlier at first, the deviations with respective to the mean motions
 236 of the rest red points will be decreased dramatically and can all be labeled as *Inlier* certainly. Thus,
 237 for each match $\langle \mathbf{f}_p, \mathbf{f}'_q \rangle$, we first evaluate its cost of assigning this match as *Outlier* as follows:

$$\begin{aligned} \text{Cost}(\mathbf{f}_p) = & \frac{\mu_p^{(x)} - \mu_{\min}^{(x)}}{\mu_{\max}^{(x)} - \mu_{\min}^{(x)}} + \frac{\mu_p^{(y)} - \mu_{\min}^{(y)}}{\mu_{\max}^{(y)} - \mu_{\min}^{(y)}} + \frac{\mu_p^{(x,y)} - \mu_{\min}^{(x,y)}}{\mu_{\max}^{(x,y)} - \mu_{\min}^{(x,y)}} + \\ & \frac{\sigma_p^{(x)} - \sigma_{\min}^{(x)}}{\sigma_{\max}^{(x)} - \sigma_{\min}^{(x)}} + \frac{\sigma_p^{(y)} - \sigma_{\min}^{(y)}}{\sigma_{\max}^{(y)} - \sigma_{\min}^{(y)}} + \frac{\sigma_p^{(x,y)} - \sigma_{\min}^{(x,y)}}{\sigma_{\max}^{(x,y)} - \sigma_{\min}^{(x,y)}}, \end{aligned} \quad (4)$$

238 where $\mu_{\min}^{(x)} = \min_p \mu_p^{(x)}$, $\sigma_{\min}^{(x)} = \min_p \sigma_p^{(x)}$, $\mu_{\max}^{(x)} = \max_p \mu_p^{(x)}$ and $\sigma_{\max}^{(x)} = \max_p \sigma_p^{(x)}$ denote the minimum
 239 and maximal mean and standard deviations in the x component of all match points in $\mathcal{M}_{\text{initial}}$,
 240 respectively, and others have the same meanings. Apparently, the black point (outlier) shown in
 241 Figure 3 has a bigger cost, and the red points (inliers) have smaller costs. Then, all match points
 242 are sorted in the decreasing order according to their costs defined in Eq. (4). In each iteration, we
 243 only check whether the top N_t matches are inliers or outliers according to the measurement defined
 244 in Eq. (3), where $N_t = \rho \times N_{\text{inlier}}(\mathcal{M}_{\text{initial}})$, ρ is the predefined proportion parameter ($\rho = 0.025$ was
 245 used in this paper) and $N_{\text{inlier}}(\mathcal{M}_{\text{initial}})$ denotes the number of matches with the label *Inlier* in $\mathcal{M}_{\text{initial}}$.
 246 We end up the iterations until the maximum number of iterations is reached or no more matches can
 247 be labeled as *Outlier*. By this way, the outliers with larger deviations with respective to neighboring
 248 points will be robustly filtered out step-by-step.

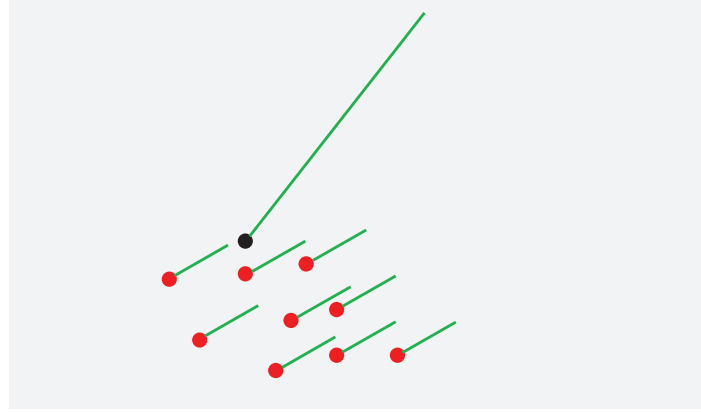


Figure 3. An visual example of outlier detection. The black point means an outlier, the red points mean inliers, and the green lines represent the motions of corresponding match points.

249 Another drawback is that the value of the parameter λ in Eq. (3) is difficult to be determined. If
 250 the value of λ is small, many inliers may be assigned as *Outlier*. In contrast, if the value of λ is big,
 251 many outliers may be assigned as *Inlier*. Thus, in this paper, we iteratively decrease the value of λ
 252 from λ_{\max} to λ_{\min} with the step λ_{step} ($\lambda_{\max} = 6$ and $\lambda_{\min} = 3$, $\lambda_{\text{step}} = 3$ were used in this paper).
 253 Namely, we first set $\lambda = \lambda_{\max}$, and perform the outlier detection process until no more outliers can be
 254 found. Then, we iteratively decrease the value of λ with a step λ_{step} , and repeat the outlier detection
 255 process until the value of λ reaches to λ_{\min} . At last, we can find all inliers from $\mathcal{M}_{\text{initial}}$ denoted as
 256 the set $\mathcal{M}_{\text{inlier}} = \{(\mathbf{f}_m, \mathbf{f}'_n) | \mathbf{f}_m \in \mathcal{F}, \mathbf{f}'_n \in \mathcal{F}'\}$.

257 2.2 Approximate Interpolation of Dense Optical Flows

Let $\bar{\mathbf{I}}$ and $\bar{\mathbf{I}}'$ be the warped images of two adjacent images \mathbf{I} and \mathbf{I}' , respectively. The aim of our proposed image warping algorithm is to ensure that the geometric alignments between the warped images $\bar{\mathbf{I}}$ and $\bar{\mathbf{I}}'$ become smaller. To achieve this objective, we propose to approximately interpolate the optical flows of all the integral pixels in $\bar{\mathbf{I}}$ with respect to \mathbf{I} and all the integral pixels in $\bar{\mathbf{I}}'$ with respect to \mathbf{I}' based on the disparity vectors of the reliable point matches with respect to each other as the control points. Firstly, we calculate the disparity vectors $\mathbf{d}(\mathbf{x}_m)$ and $\mathbf{d}(\mathbf{x}'_n)$ of each reliable point match $\langle \mathbf{x}_m, \mathbf{x}'_n \rangle$ in $\mathcal{M}_{\text{inlier}}$ from the warped images to the original ones as follows:

$$\begin{cases} \mathbf{d}(\mathbf{x}_m) = \frac{1}{2}(\mathbf{x}_m - \mathbf{x}'_n) = \frac{1}{2}(x_m - x'_n, y_m - y'_n)^\top, \\ \mathbf{d}(\mathbf{x}'_n) = \frac{1}{2}(\mathbf{x}'_n - \mathbf{x}_m) = \frac{1}{2}(x'_n - x_m, y'_n - y_m)^\top, \end{cases} \quad (5)$$

258 where $\mathbf{x}_m = (x_m, y_m)^\top$ and $\mathbf{x}'_n = (x'_n, y'_n)^\top$. By this way, we expect to warp the images \mathbf{I} and \mathbf{I}' based
 259 on the half offsets of real disparity vectors to reduce the warping distortion.

260 Secondly, we propose to approximately interpolate the optical flows of all integral pixels in
 261 the warped images $\bar{\mathbf{I}}$ and $\bar{\mathbf{I}}'$ based on the disparity vectors $\{\mathbf{d}(\mathbf{x}_m)\}_{\mathbf{x}_m \in \mathcal{M}_{\text{inlier}}}$ and $\{\mathbf{d}(\mathbf{x}'_n)\}_{\mathbf{x}'_n \in \mathcal{M}_{\text{inlier}}}$
 262 of the control points $\{\mathbf{x}_m - \mathbf{d}(\mathbf{x}_m)\}_{\mathbf{x}_m \in \mathcal{M}_{\text{inlier}}}$ and $\{\mathbf{x}'_n - \mathbf{d}(\mathbf{x}'_n)\}_{\mathbf{x}'_n \in \mathcal{M}_{\text{inlier}}}$, respectively. This problem
 263 can be formulated as the scattered data interpolation problem. Due to the sparsity of the control
 264 points, in this paper we adapt to apply the Multilevel B-Splines Approximation (MBA) [37] to solve
 265 this problem, which has been widely used for image registration, image morphing, image warping,
 266 curve/surface fitting and geometric modeling. By this MBA interpolation, we separately interpolate
 267 the horizontal and vertical components of optical flows (i.e., disparity vectors) of all the integral pixels
 268 in $\bar{\mathbf{I}}$ and $\bar{\mathbf{I}}'$, respectively. In this way, we finally obtain the dense optical flows $\mathcal{D}(\bar{\mathbf{I}}) = \{\tilde{\mathbf{d}}(\mathbf{p})\}_{\mathbf{p} \in \bar{\mathbf{I}}}$ and

269 $\mathcal{D}(\bar{I}') = \{\tilde{\mathbf{d}}(\mathbf{p}')\}_{\mathbf{p}' \in \bar{I}'}$ of all the integral pixels $\{\mathbf{p}\}_{\mathbf{p} \in \bar{I}}$ and $\{\mathbf{p}'\}_{\mathbf{p}' \in \bar{I}'}$ in the warped images \bar{I} and \bar{I}' with
 270 respective to the original images I and I' , respectively.

271 2.3 Two Image Warping

272 Here, we demonstrate how to generate the warped image \bar{I} from the original image I based on
 273 the dense optical flows $\mathcal{D}(\bar{I})$ of \bar{I} with respect to I , and the generation of the warped image \bar{I}' is
 274 similar. For each pixel $\mathbf{p} \in \bar{I}$, we can easily calculate its corresponding 2D position in I based on its
 275 approximately interpolated optical flow (i.e., disparity vector) $\tilde{\mathbf{d}}(\mathbf{p})$ as $\mathbf{p} + \tilde{\mathbf{d}}(\mathbf{p})$. Then, we use the
 276 bilinear interpolation algorithm to interpolate the intensity of the corresponding point $\mathbf{p} + \tilde{\mathbf{d}}(\mathbf{p})$ in I
 277 as the intensity of the integral pixel $\mathbf{p} \in \bar{I}$.

278 According to the above image warping procedure, we can obtain two warped images from two
 279 input panoramic images with the overlap. The geometric misalignments between warped images
 280 become smaller than those between the original images after warping correction.

281 2.4 Multiple Image Warping

282 Until now, we have introduced how to warp two images based on the optical flows. But, we
 283 need to warp multiple input images to generate the last panorama. In the experimental results
 284 presented in this paper, the input images are comprised of 5 horizontal ones and 1 vertical one,
 285 which are represented as $(I_1, I_2, I_3, I_4, I_5, I_6)$ whose correspondingly warped images are represented
 286 as $(\bar{I}_1, \bar{I}_2, \bar{I}_3, \bar{I}_4, \bar{I}_5, \bar{I}_6)$, and the overlap relationship of those images is shown in Figure 9. For this
 287 particular case, here we will detailedly introduce how to warp these six images for producing the
 288 last panorama before color correction. Other cases of multiple images can be handled in a similar
 289 way. For multiple input panoramic images, we first collect all image pairs according to their overlap
 290 relationship as shown in Figure 9. Obviously, there are five image pairs along the horizontal direction,
 291 and one image pair along the vertical direction. We first handle the horizontal image pairs and
 292 then deal with the vertical image pair. For each horizontal image pair, we match them one by one
 293 by the method presented in Section 2.1, as an illustrative example shown in Figure 4, from which
 294 we can find that one horizontal image is overlapped with two adjacent images in the horizontal
 295 direction. For example, for the image I_1 , it overlaps with I_2 and I_5 , respectively, so we need to collect
 296 all matching points from these two overlap regions as the control points for warping I_1 . The dense
 297 optical flow field of the warped image \bar{I}_1 with respect to the original image I_1 can be approximately
 298 interpolated based on those control points via the MBA algorithm. Therefore, five horizontal warped
 299 images $\bar{I}_1, \bar{I}_2, \bar{I}_3, \bar{I}_4$ and \bar{I}_5 can be generated by warping their corresponding original images according
 300 to the method presented in Section 2.3, respectively. Figure 5 shows an example for warping one
 301 horizontal image. After that, we generate the bottom blended image I_H by blending all horizontal
 302 warped images according to the proposed color correction method presented in Section 3 and the
 303 adopted image mosaicking strategy described in Section 4. Finally, to produce the last panorama, the
 304 top image I_6 and the horizontal blended image I_H will be warped according to those matching points
 305 as the control ones.

306 3 Color Correction

307 The large geometric misalignments can be efficiently eliminated by our proposed image warping
 308 algorithm, but there also exist the color differences between the warped images, so the stitching
 309 artifacts are still visible. Generally, the image blending technique can solve it easily by smoothing
 310 the color along the seamlines. However, it does not work well for input images with very large
 311 color differences. The simple image blending maybe can not efficiently conceal the artifacts if we
 312 don't magnificently correct color differences between images in advance, which results in low-quality

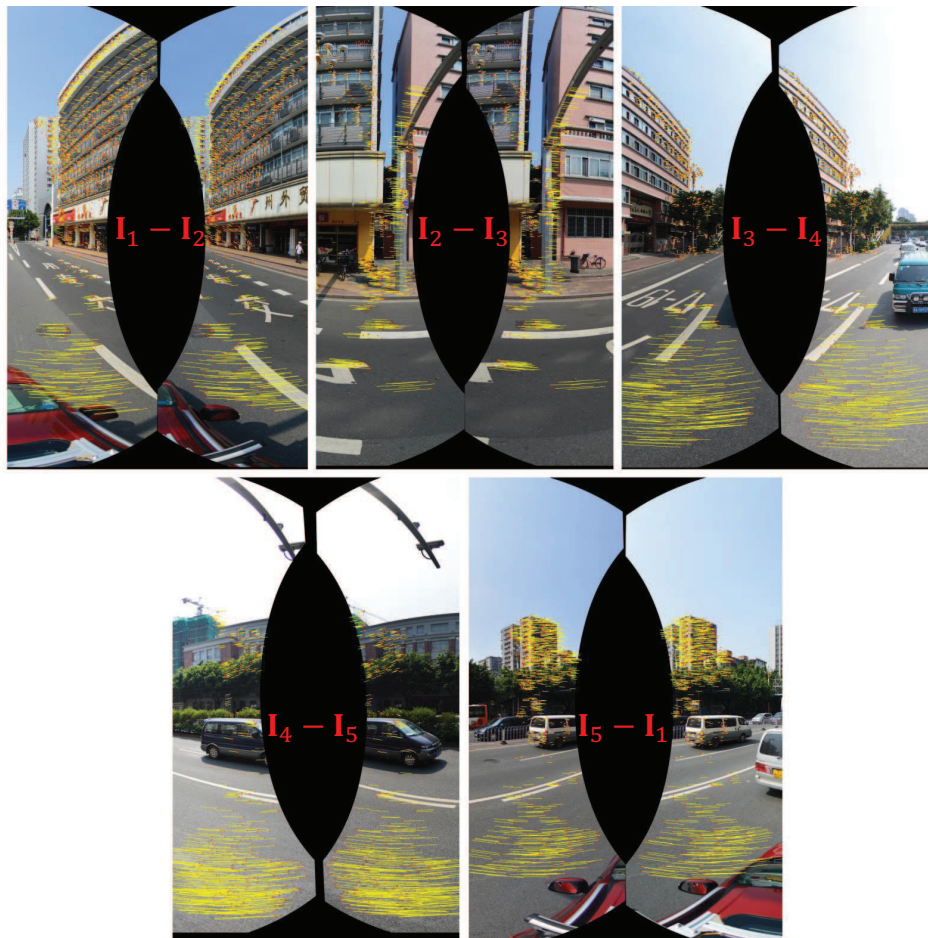


Figure 4. The feature matching results of all five horizontal image pairs in the overlap regions.

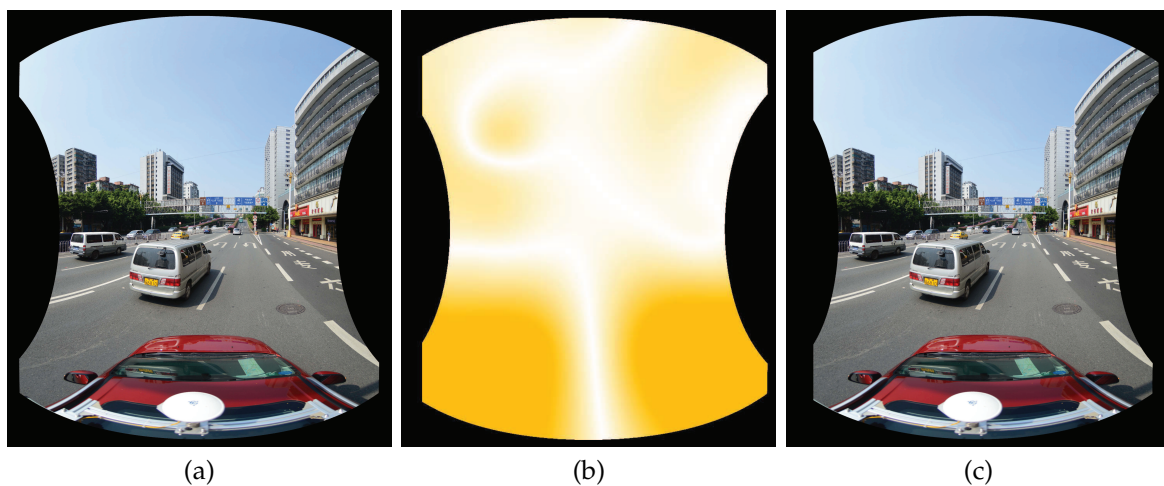


Figure 5. An illustrative example of image warping: (a) the original aligned image; (b) the dense optical flows approximately interpolated by the MBA algorithm; (c) the last warped image. In (b), the deeper orange means the larger disparity.

313 panoramic images, as an illustrative example shown in Figure 6. In addition, the large color
 314 differences maybe also affect the quality of the detected seamlines. Thus, in this paper, we propose
 315 to reduce the color differences between warped images before the optimal seamlines are detected.

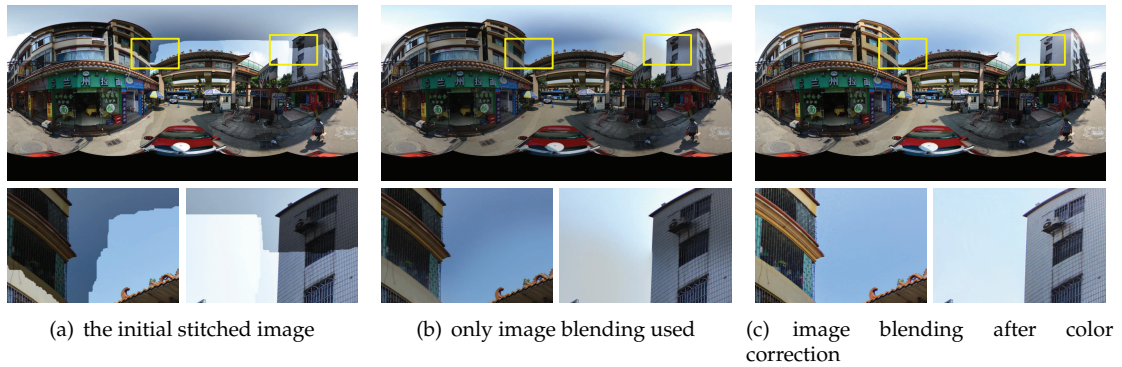


Figure 6. An example of our proposed color correction strategy used to improve the panorama stitching quality before apply the image blending.

316 Generally, the color differences should be also corrected before the image warping step to ensure
 317 the quality of feature matching results. But our adopted SURF feature matching algorithm is robust
 318 enough to the large photometric inconsistencies, so there are no obvious influence on our algorithm
 319 if we apply the color correction after image warping.

320 In this paper, we first apply the automatic contrast adjustment to reduce the brightness
 321 differences between images and then propose a novel and efficient color correction algorithm via
 322 matching extreme points of intensity histograms to further reduce the color differences. For the
 323 overlap image regions between two images, we construct their own Probability Density Functions
 324 (PDFs) and Cumulative Distribution Functions (CDFs) with respect to the intensity histograms in
 325 the three HSV channels, respectively. One way to eliminate color differences is to ensure that the
 326 three CDFs of the overlap regions in the first image in the three HSV channels are approximately
 327 same to those CDFs of the overlap regions in the second image, respectively. Obviously, we can
 328 correct the CDFs based on several uniformly spaced knots as [54] did. However, due to the existence
 329 of geometric misalignments, the scenes presented by two images in the overlap regions are not
 330 completely consistent. To solve this problem, we replace the knots by the matched extreme points
 331 extracted from the two PDFs. If the number of matched extreme points is not sufficient, we will
 332 suitably introduce those uniformly space knots. At last, the intensities of all the pixels in the two
 333 images are modified afterwards based on the matched extreme points extracted from the PDFs, not
 334 only for the pixels in the overlap regions, but also in the non-overlap regions.

3.1 Automatic Contrast Adjustment

At first, in order to make sure that multiple images have the similar contrast, which can produce satisfactory blending results, the three RGB channels of individual images are automatically adjusted in contrast. The histograms of a color image are calculated firstly in each of the three RGB channels, respectively. Let \mathbf{I} be a single-channel image and $\mathbb{I} = \{I_k\}_{k=1}^N$ be a set of one dimensional sorted intensities of all valid pixels in \mathbf{I} in the ascending order where N denotes the total number of valid pixels in \mathbf{I} and I_k represents the intensity of the k -th sorted pixel in \mathbf{I} . The minimal and maximal intensities I_{\min} and I_{\max} in \mathbf{I} are defined, respectively, as follows:

$$I_{\min} = I_{\lceil N \times c\% \rceil} \quad \text{and} \quad I_{\max} = I_{\lceil N \times (1-c\%) \rceil}, \quad (6)$$

where $\lceil \Delta \rceil$ denotes the upper integer of a real value Δ and c is a small percentage value in the range of $(0, 50)$ ($c = 0.1$ was empirically used in this paper), which can be used to skip over a part of the real minimal and maximal intensities due to the fact that these pixels may be caused by noises and information lacking in most cases. The minimal and maximal intensity values of

the R , G and B channels of a color image are denoted as R_{\min} , G_{\min} , B_{\min} , R_{\max} , G_{\max} , and B_{\max} , respectively. The minimal and maximal intensity values of the whole color image are defined as $V_{\min} = \min(R_{\min}, G_{\min}, B_{\min})$ and $V_{\max} = \max(R_{\max}, G_{\max}, B_{\max})$, respectively. Therefore, any intensity I of the R , G and B channels of a color image will be modified as:

$$I' = \begin{cases} 0, & I \leq V_{\min}, \\ 255 \times \frac{I - V_{\min}}{V_{\max} - V_{\min}}, & V_{\min} < I < V_{\max}, \\ 255, & I \geq V_{\max}. \end{cases} \quad (7)$$

336 In the same way, all the images to be used for creating a panorama will be automatically adjusted in
337 contrast, which will slightly reduce the brightness differences between images.

338 3.2 Finding Extreme Points

339 After applying the automatic contrast adjustment on the multiple panoramic images, we propose
340 to further reduce the color differences between panoramic images by matching extreme points of
341 histograms. For the statistic analysis, only valid pixels in the overlap regions between two images are
342 considered. Let \mathbf{A} and \mathbf{B} be the overlap image regions in two images, respectively. To make a better
343 description of the information hidden behind the image, we convert \mathbf{A} and \mathbf{B} from the original RGB
344 color space to the HSV color space, respectively. For each channel of \mathbf{A} and \mathbf{B} , we calculate their PDFs
345 and CDFs, which are denoted as \mathbf{PDF}_A , \mathbf{PDF}_B , \mathbf{CDF}_A , and \mathbf{CDF}_B , respectively.

346 To robustly find extreme points in both \mathbf{PDF}_A and \mathbf{PDF}_B , these two PDFs are smoothed first by
347 a Gaussian function to suppress possible noise. The initial local extreme points can be easily obtained
348 from the smoothed \mathbf{PDF}_A and \mathbf{PDF}_B . In an ideal situation, the extreme points should be uniformly
349 distributed in the color space. However, most of the extreme points are relatively centralized in some
350 cases, which will lead to the information redundancy due to that multiple extreme points are selected
351 out to represent the similar image statistical information. To avoid the situation mentioned above,
352 we further checkout all initial extreme points by the local window suppression. Let $\{L_A^i\}_{i=1}^K$ be the
353 intensities of K extreme points $\{P_A^i\}_{i=1}^K$ in \mathbf{PDF}_A , which are sorted in the ascending order. Given an
354 extreme point P_A^i , we generate a neighborhood range $[L_A^i - w, L_A^i + w]$ centered on the corresponding
355 intensity L_A^i with the size of $(2w + 1)$. We set $w = 2$ if not specifically stated in this paper. If there
356 exist more than one extreme points located in this neighborhood range, the extreme point with the
357 highest frequency in \mathbf{PDF}_A will be retained and other extreme points will be removed. All initial
358 extreme points are checked in this way and the retained extreme points are used for the following
359 matching. The final extreme points extracted from \mathbf{PDF}_A and \mathbf{PDF}_B are represented as $\{\mathbf{P}_A^i\}_{i=1}^{N_A}$ and
360 $\{\mathbf{P}_B^j\}_{j=1}^{N_B}$, where N_A and N_B are the numbers of extreme points in \mathbf{PDF}_A and \mathbf{PDF}_B , respectively. For
361 each extreme point \mathbf{P} , it consists of 4 components according to $\mathbf{P} = \{F, L, \hat{C}, \check{C}\}$ where F denotes
362 the frequency of this point in PDF, L represents the corresponding intensity, and \hat{C} and \check{C} means the
363 cumulative values of the intensities $(L + \varepsilon)$ and $(L - \varepsilon)$ in CDF (we set $\varepsilon = 2$ if not specifically stated
364 in this paper).

365 3.3 Matching Extreme Points

The extreme points can sufficiently reflect image statistical characteristics. To efficiently adjust the color differences, one way is to ensure that the intensities of corresponding extreme points are the same. Thus, we should match the extreme points firstly. To reliably match these extreme points

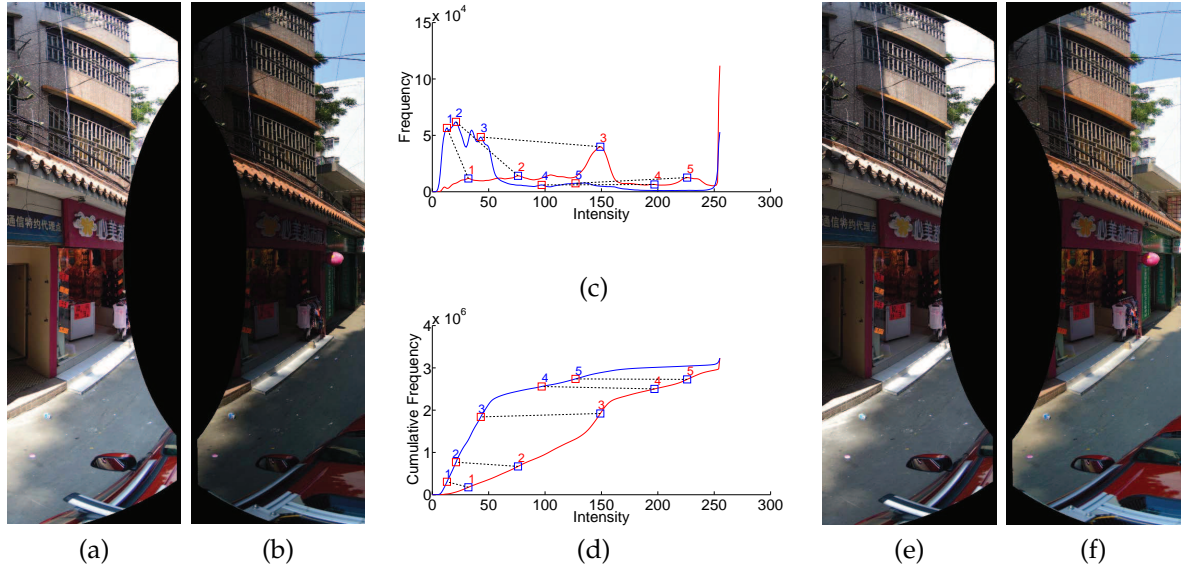


Figure 7. A visual example of our proposed color correction approach: (a)-(b) the overlap image regions of the input left and right images, respectively; (c)-(d) the curves of PDF and CDF in one channel where the red curves stand for the left image and the blue ones stand for the right image, and the matched peaks are marked by the same number and connected by the black dotted lines; (e)-(f) the corrected left and right images, respectively.

$\{\mathbf{P}_A^i\}_{i=1}^{N_A}$ and $\{\mathbf{P}_B^j\}_{j=1}^{N_B}$, we define a cost function to measure the matching similarity of two extreme points \mathbf{P}_A^i and \mathbf{P}_B^j as:

$$\text{Cost}(\mathbf{P}_A^i, \mathbf{P}_B^j) = \frac{F_A^i + F_B^j}{2F_{\max}} \times \frac{\min(F_A^i, F_B^j)}{\max(F_A^i, F_B^j)} \times \frac{\max(\hat{C}_A^i - \check{C}_A^i, \hat{C}_B^j - \check{C}_B^j)}{\max(\hat{C}_A^i, \hat{C}_B^j) - \min(\check{C}_A^i, \check{C}_B^j)}, \quad (8)$$

where F_{\max} is the maximal frequency of all the extreme points in both \mathbf{PDF}_A and \mathbf{PDF}_B . The above cost function judges the two extreme points from the view of both PDF and CDF. The first term $\frac{F_A^i + F_B^j}{2F_{\max}}$ indicates that those possibly matched extreme points with the higher frequencies generates higher costs, which may be peaked out first in the following matching selection strategy. The second term $\frac{\min(F_A^i, F_B^j)}{\max(F_A^i, F_B^j)}$ indicates that there are the similar frequencies for two possibly matched extreme points \mathbf{P}_A^i and \mathbf{P}_B^j . The last term is applied to ensure that the accumulative values of two possibly matched extreme points \mathbf{P}_A^i and \mathbf{P}_B^j are approximate. From this term, we can find that if the small range of cumulative values of two extreme points are similar, the numerator $\max(\hat{C}_A^i - \check{C}_A^i, \hat{C}_B^j - \check{C}_B^j)$ is close to the denominator $\max(\hat{C}_A^i, \hat{C}_B^j) - \min(\check{C}_A^i, \check{C}_B^j)$, which results in that this term is close to 1. In contrast, if the numerator is smaller and the denominator is larger, this term will approach to 0. In summary, if the frequencies of two extreme points are larger and more similar, and the accumulative values of those points are more approximate, their matching cost is bigger. In contrast, it is smaller. The higher the cost function value is, the more likely these two extreme points are matched. Based on this cost definition, a $N_A \times N_B$ matching cost matrix $\mathbf{M} = [M_{ij}]_{N_A \times N_B}$ is created. In order to efficiently eliminate the impossibly matched extreme points, we empirically designed three hard conditions

from the view of both PDF and CDF to check whether two extreme points \mathbf{P}_A^i and \mathbf{P}_B^j are possibly matched as follows:

$$\begin{cases} \frac{\min(F_A^i, F_B^j)}{\max(F_A^i, F_B^j)} < \theta_f, \\ \check{C}_A^i > \hat{C}_B^j + \theta_c \times C_{\max}, \\ \check{C}_B^j > \hat{C}_A^i + \theta_c \times C_{\max}, \end{cases} \quad (9)$$

where θ_f and θ_c are two empirical thresholds ($\theta_f = 0.25$ and $\theta_c = 0.02$ were used in this paper), C_{\max} is the maximal value of CDF, namely, the valid pixel number of overlap regions. The matching cost $Cost(\mathbf{P}_A^i, \mathbf{P}_B^j)$ is set to zero, i.e., $M_{ij} = Cost(\mathbf{P}_A^i, \mathbf{P}_B^j) = 0$, if at least one of the above three conditions is not met, namely, \mathbf{P}_A^i and \mathbf{P}_B^j are not possibly matched. From the view of PDF, the first condition indicates that the frequencies of the two possibly matched extreme points \mathbf{P}_A^i and \mathbf{P}_B^j should be a relatively small difference. From the view of CDF, the second and third conditions indicate that \mathbf{P}_A^i and \mathbf{P}_B^j are possibly matched if their corresponding CDF values are approximate. According to the above three hard conditions, the matching cost matrix \mathbf{M} will be updated, in which all the zero elements indicate that they are not possibly matched.

Based on the computed matching cost matrix \mathbf{M} , we propose an efficient iterative strategy to find the matched extreme points as the following steps:

- Step 1: Finding the highest non-zero cost element M_{ij} from the matrix \mathbf{M} and its corresponding extreme points \mathbf{P}_A^i and \mathbf{P}_B^j is selected out as a reliable extreme point match.
- Step 2: Updating the matrix \mathbf{M} by removing the i -th row and the j -th column due to that \mathbf{P}_A^i and \mathbf{P}_B^j have been successfully matched.
- Step 3: Performing the above two steps iteratively until the updated matrix \mathbf{M} is empty or there exists no non-zero element in \mathbf{M} .

By the above iterative strategy, a set of reliable extreme point matches will be found. In Figure 7, we have shown a visual example of our proposed color correction approach. The input two images have large color differences in overlap regions, as shown in Figures 7(a)-(b). We find 5 matched extreme points in PDF of one channel. Based on those correspondences, the large color differences can be eliminated, as shown in Figures 7(e)-(f). From this example, we can find that our proposed approach can handle the images with large color differences very well.

Sometimes, no match or too few matches can be reliably found via the above matching strategy in the whole CDF range or some relatively large CDF range. In this case, we will introduce more matches with the help of both \mathbf{CDF}_A and \mathbf{CDF}_B , which are selected from H uniformly distributed points $\{C_A^k\}_{k=1}^H$ and $\{C_B^k\}_{k=1}^H$ from \mathbf{CDF}_A and \mathbf{CDF}_B , respectively, but not from the previously found extreme points. The same number of sampling points in \mathbf{CDF}_A and \mathbf{CDF}_B are uniformly selected in accordance with the cumulative density values. In our experiments, the percentages of sampling intervals were used as [0.1, 0.3, 0.5, 0.7, 0.9]. If there exists no extreme point match found in the ranges $[C_A^k - \kappa C_{\max}, C_A^k + \kappa C_{\max}]$ and $[C_B^k - \kappa C_{\max}, C_B^k + \kappa C_{\max}]$, the current sampling points C_A^k and C_B^k will be added into the matching set as a new point match, where κ is a given threshold in advance ($\kappa = 0.1$ was used in this paper).

3.4 Correcting Color Difference

The extracted matching points in the overlap image regions are then applied to correct the intensities of two adjacent images, including the pixels in non-overlap regions. Let $\{Q_A^k\}_{k=1}^N$ and $\{Q_B^k\}_{k=1}^N$ be the final matching points in CDFs in the overlap regions \mathbf{A} and \mathbf{B} with N point matches. Based on the matching results, the intensities of the matching points Q_A^k and Q_B^k are modified to $(L_A^k + L_B^k)/2$ where L_A^k and L_B^k denote the intensities of k -th match (Q_A^k, Q_B^k) in CDFs, respectively. In this way, the intensities of $\{(Q_A^k, Q_B^k)\}_{k=1}^N$ are corrected to $\{(\hat{L}_A^k, \hat{L}_B^k)\}_{k=1}^N$, respectively, where

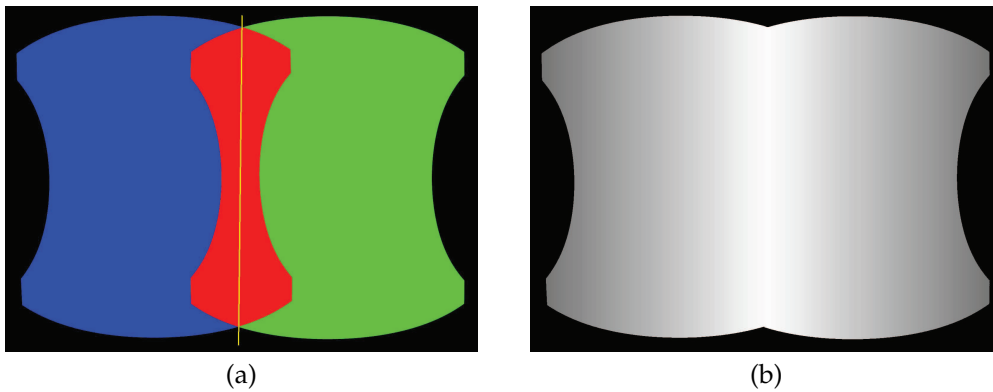


Figure 8. An illustration of the alpha weighting fusion map of two adjacently warped images: (a) two overlapped images represented by the blue and green regions, respectively, with the overlap image region marked in red and the center line marked in yellow; (b) the normalized alpha weighting fusion map for two images where the brighter regions indicate higher values.

$\hat{L}_A^k = \hat{L}_B^k = (L_A^k + L_B^k)/2$. Based on these corrections, the intensity of any pixel in both **A** and **B** will be adjusted linearly. For example, given a pixel $\mathbf{p} \in \mathbf{A}$ whose intensity $L_A(\mathbf{p})$ will be linearly corrected as:

$$\hat{L}_A(\mathbf{p}) = \hat{L}_A^l + (L_A(\mathbf{p}) - L_A^l) \frac{\hat{L}_A^u - \hat{L}_A^l}{L_A^u - L_A^l}, \quad (10)$$

where $L_A(\mathbf{p}) \in [L_A^u, L_A^l]$, L_A^u and L_A^l denote the intensities of two matching points in **A** that are closest to $L_A(\mathbf{p})$, and the \hat{L}_A^u and \hat{L}_A^l are the corresponding corrected intensities. In order to produce a smooth and gradual transition from non-overlap regions to overlap ones, the alpha correction method is conducted as:

$$L'_A(\mathbf{p}) = (1 - \alpha(\mathbf{p}))L_A(\mathbf{p}) + \alpha(\mathbf{p})\hat{L}_A(\mathbf{p}), \quad (11)$$

400 where $L'_A(\mathbf{p})$ denotes the finally fused intensity of the pixel \mathbf{p} , $L_A(\mathbf{p})$ is the original intensity of
 401 the pixel \mathbf{p} while $\hat{L}_A(\mathbf{p})$ is the corrected intensity of the corresponding pixel based on the above
 402 mentioned correction method, and $\alpha(\mathbf{p})$ is a function that related to the distance between the pixel \mathbf{p}
 403 and the center line of the overlap image region, which ranges between 0 and 1 as shown in Figure 8
 404 where the smaller the distance to the center line is, the larger the α is. All the pixels in another image
 405 will be processed in the same way.

406 4 Image Mosaicking

407 Although the large geometric misalignments and photometric inconsistencies have been greatly
 408 reduced through our proposed image warping and color correction algorithms, respectively, there
 409 always exist small geometric misalignments and color differences between adjacent images. To stitch
 410 the color corrected panoramic images into the single composite panorama, we also need to find the
 411 optimal seamlines in the overlap image regions between warped images to magnificently conceal the
 412 parallax. Furthermore, an efficient image blending algorithm will be further applied to eliminate the
 413 stitching artifacts caused by small color differences along the seamlines.

414 4.1 Optimal Seamline Detection

415 In this paper, the optimal seamlines between color corrected images will be efficiently extracted
 416 using the graph-cuts-based seamline detection algorithm presented in [19]. This novel algorithm is
 417 used to efficiently detect optimal seamlines for mosaicking street-view panoramic images without
 418 precisely common center in a two-label graph cuts energy minimization framework. This algorithm

419 magnificently fuses the information of image color, gradient, and texture complexity into the data
420 and smooth energy terms in graph cuts to effectively ensure that the seamlines are optimally
421 detected in the laterally continuous regions with high image similarity and low object dislocation
422 to magnificently conceal the parallax between images. For multiple images, we apply the traditional
423 *frame-to-frame optimization* strategy to efficiently find all optimal seamlines. The details of this strategy
424 are described in Section 3.1 of [19]. The experimental results on a large set of images reported in [19]
425 have demonstrated that this algorithm is capable of creating high-quality seamlines for multiple
426 image mosaicking, while not crossing majority of visually obvious foreground objects and most of
427 overlap regions with low image similarity to effectively conceal the image parallax at different extents.

428 4.2 Image Blending

429 Although the major color differences are eliminated between input images by applying our
430 proposed color correction strategy presented in Section 3, there still exist the artifacts along the
431 seamlines due to that the color differences can not be removed completely via color correction. Thus,
432 a good image blending algorithm is needed to generate the last pleasant panorama. To quickly blend
433 the color corrected images after detecting the optimal seamlines, the transition smoothing methods
434 (also known as feathering [47] or alpha blending methods [48]) can be used to minimize the visibility
435 of seamlines by smoothing the common overlapping regions of the combined images. However, to
436 produce a more pleasant panorama, in this paper, we use the Laplacian pyramid blending [49] to
437 stitch multiple color corrected images at one time.

438 5 Experimental Results

439 Extensive experiments on representative street-view panoramic images were conducted to
440 comprehensively evaluate the performance of our proposed unified framework for street-view
441 panorama stitching. In our paper, all used street-view panoramic images were captured from the
442 real world scenes by an integrated multi-camera equipment with six Nikon D7100 cameras of 24
443 million pixels with wide-angle lenses mounted on a mobile vehicle platform. Six camera images
444 were aligned into a common spherical coordinate system with the image size of 12000×6000 pixels.
445 Due to that the projection centers of these six cameras are not precisely the same, there always
446 exist large geometrical misalignments at different extents between the adjacently aligned images,
447 especially in the image regions close to the camera centers. The overlap relationship of those six
448 panoramic images is shown in Figure 9. Our algorithms in this paper were implemented with
449 C++ under Windows and tested in a computer with an Intel Core i7-4770 at 3.4GHz and the 16GB
450 RAM memory. Due to the limit of pages, more experimental results and analysis are presented at
451 <http://cvrs.whu.edu.cn/projects/PanoStitching/>.

452 5.1 Image Warping

453 In this section, we conducted the experiments on two groups of panoramic images to prove
454 the effectiveness and superiority of our proposed image warping algorithm described in Section 2.
455 The panorama stitching results without and with the use of our proposed image warping algorithm
456 in the first group of six panoramic images are shown in Figures 10(a) and (b), respectively. We
457 can find that the whole seamlines in two panoramas cross the similar regions with the high image
458 similarity. However, from the whole stitching results and especially the detailed local regions shown
459 in Figures 10(a) and (b), we observed that the stitching artifacts caused by the geometric dislocation
460 in the panorama, as shown in Figure 10(a), stitched without the use of image warping algorithm
461 are more obvious than the panorama, as shown in Figure 10(b), stitched with its use. Noticeably,
462 the stitching artifacts caused by geometric dislocation become smaller as expected when the image



Figure 9. The image overlap regions of six geometrically aligned and warped images in the 360° street-view panoramic view where the black, the green and the red stand for the no-overlapped, two-overlapped, multi-overlapped image regions, respectively.

463 warping algorithm was applied, as shown in Figure 10(b). While not using the image warping
 464 algorithm, the geometric dislocation is very large, as shown in Figure 10(a). For example, in the
 465 first enlarged local region, the seamline crossed the text without the used of image warping, and it
 466 avoided crossing the text when the image warping was used. In the second enlarged local region,
 467 although two seamlines crossed the road with pavement stairs, we can find that the dislocation
 468 is almost invisible in the pavement stairs when the image warping was used, but it is so obvious
 469 without the use of the image warping. In the aspect of computational cost, without the use of image
 470 warping, our algorithm took around 17.89s in the above experiment, only the elapsed time in six
 471 optimal seamlines detection is included. However, with its use, our algorithm took around 70.93s
 472 consisting of all the elapsed times in the image warping and the optimal seamline detection. From this
 473 comparison, we observed that the seamline detection is efficient, but the image warping is relatively
 474 time-consuming. This is mainly because that we need to find the inlier matches for all image pairs at
 475 first and then interpolate the dense optical flows by MBA for each image, which is time-consuming.
 476 But our proposed image warping algorithm can significantly improve the quality of the last stitched
 477 panorama.

478 The comparative experimental results on another group of panoramic images are presented in
 479 Figures 10(c) and (d), respectively, and the similar conclusions can be drawn. The computational
 480 times of our algorithm without the use of image warping and with its use are 13.19s and 56.77s,
 481 respectively.

482 From the above experimental results on two groups of panoramic images, we observed that
 483 our proposed image warping algorithm can effectively eliminate the stitching artifacts caused by the
 484 geometrical dislocations and can also slightly improve the quality of the found optimal seamlines to
 485 some extent.

486 5.2 Color Correction and Image Blending

487 In this section, we conducted the experiments in two group panoramic images to prove that our
 488 proposed color correction algorithm can magnificently reduce the large color differences between the
 489 warped images. In addition, we also presented the last panoramas generated by our proposed system
 490 and compared them with the open-source software *Enblend*⁴ which are popularly used to generate
 491 the street-view panorama by stitching the registered panoramic images.

⁴ Available at <http://enblend.sourceforge.net/>.

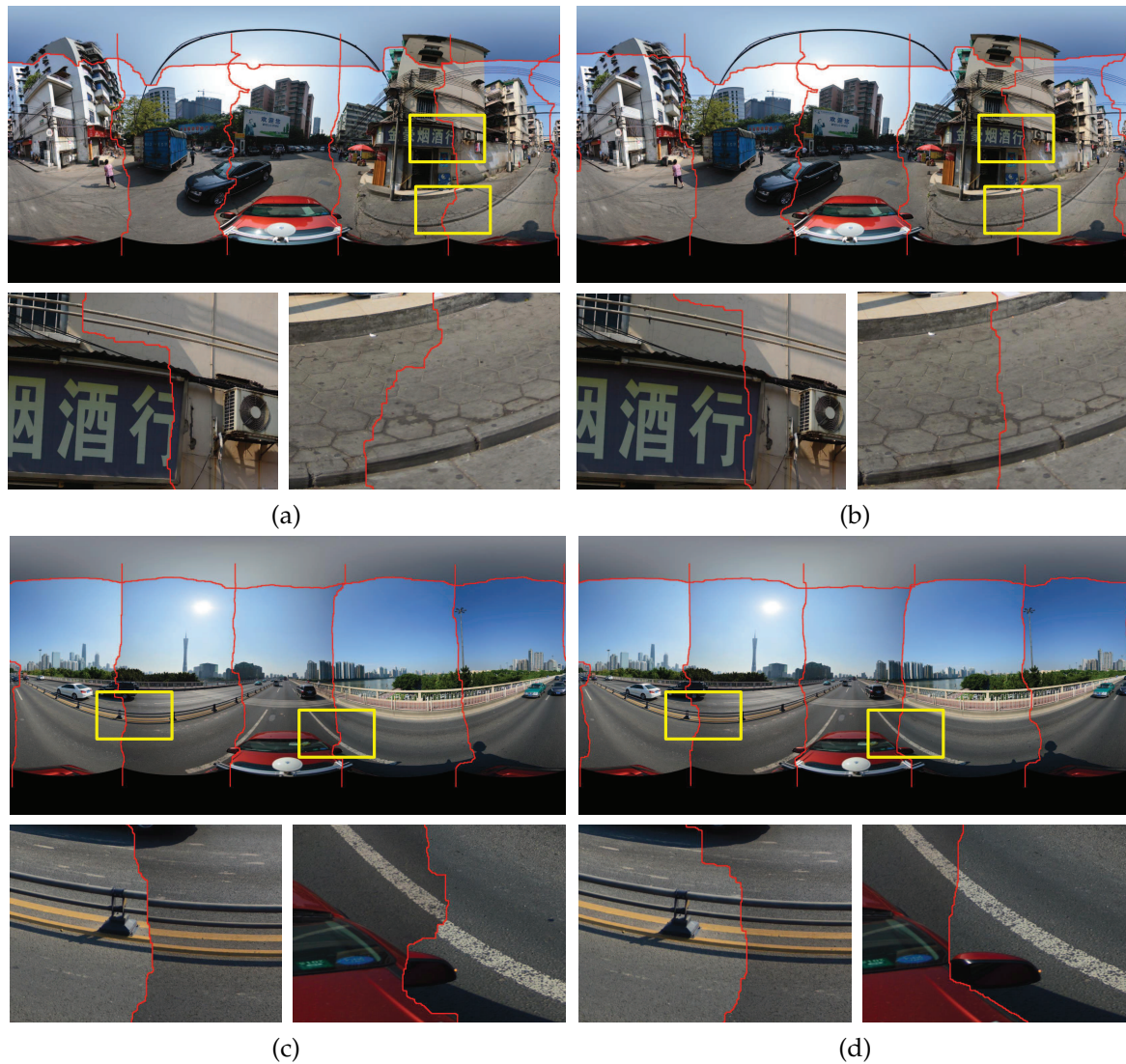


Figure 10. Visual comparison of the stitching results with the optimal seamlines in two groups of six panoramic images when our proposed image warping algorithm was used (Right:(b) and (d)) or not (Left: (a) and (c), namely, the stitching results of [19]). The red lines stand for the detected optimal seamlines between images.

492 Figure 11 shows the experimental results on the first group of panoramic images. The panorama
 493 stitching results without and with the use of color correction are shown in Figures 11(a) and (b),
 494 respectively. From the whole stitching results and especially the detailed local regions shown in
 495 Figures 11(a) and (b), we can find that color differences between the warped images were significantly
 496 reduced and are almost invisible. In addition, the quality of the detected optimal seamlines was
 497 improved as expected when the color correction algorithm was used due to that the color differences
 498 were greatly reduced before the seamlines were found. For example, the seamline rounded the
 499 advertising board instead of crossing it when the color correction algorithm was used, as shown in
 500 the detailed image regions in Figures 11(a) and (b). In the aspect of computational cost, without the
 501 use of the color correction, our algorithm took around 18.01s to find all six optimal seamlines. With its
 502 use, our algorithm took around 33.52s to correct the color differences and find the optimal seamlines,
 503 means that the color correction algorithm took around 15.51s. To generate the last panorama, the
 504 Laplacian pyramid blending algorithm was further applied, whose generated result is shown in
 505 Figure 11(d). And in Figure 11(c), we also present the last panorama generated by *Enblend*. From

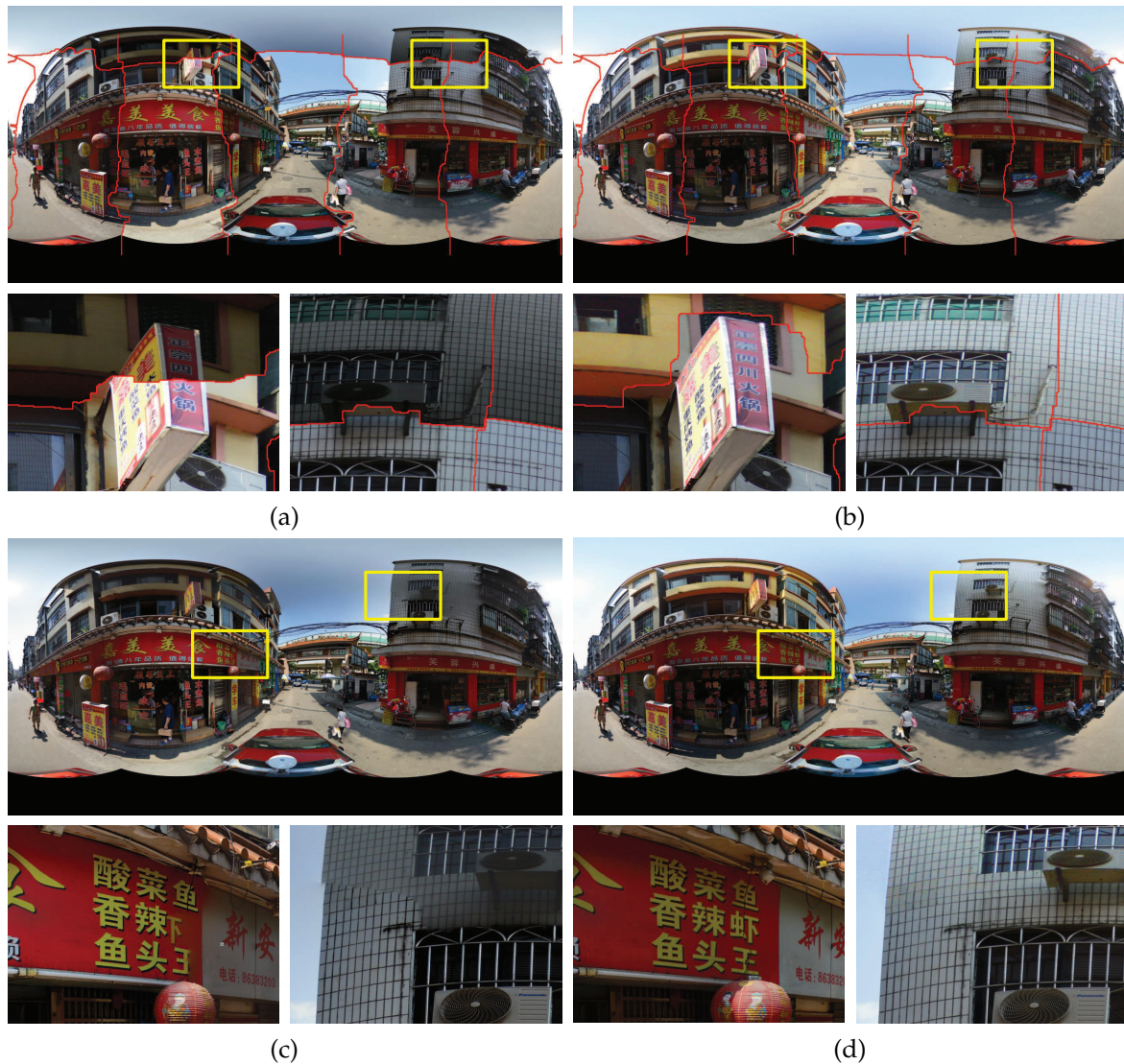


Figure 11. Visual comparison in the first group of six panoramic images: (a)-(b) the stitching results with the optimal seamlines when the our proposed color correction was used (b) or not (a); (c)-(d) the last panoramas generated by *Enblend* (c) and our proposed stitching system (d).

506 the visual comparison, we can observe that our proposed stitching system with image warping
 507 and color correction obviously outperforms *Enblend*. Noticeably, the stitching artifacts caused by
 508 geometric misalignments and photometric inconsistencies still exist in the panorama generated by
 509 *Enblend*, as shown in Figure 11(c) but they almost disappeared in our produced panorama, as shown
 510 in Figure 11(d). In the aspect of computational cost, the Laplacian pyramid blending algorithm took
 511 35.56s.

512 The experimental results on another group of panoramic images are presented in Figure 12
 513 and the similar conclusion can be drawn. The large color differences were greatly reduced by our
 514 proposed color correction algorithm, especially in the regions of sky and the tall buildings, and
 515 the quality of the detected seamlines was slightly improved to some extent. The seamlines bypass
 516 the buildings and the white lane when the color differences were corrected for the warped images.
 517 Likewise, the stitching artifacts existed in the panorama produced by *Enblend* disappeared in the
 518 panorama generated by our proposed system. The elapsed times in color correction, optimal seamline
 519 detection and image blending are 17.33s, 13.77s, and 35.61s, respectively.

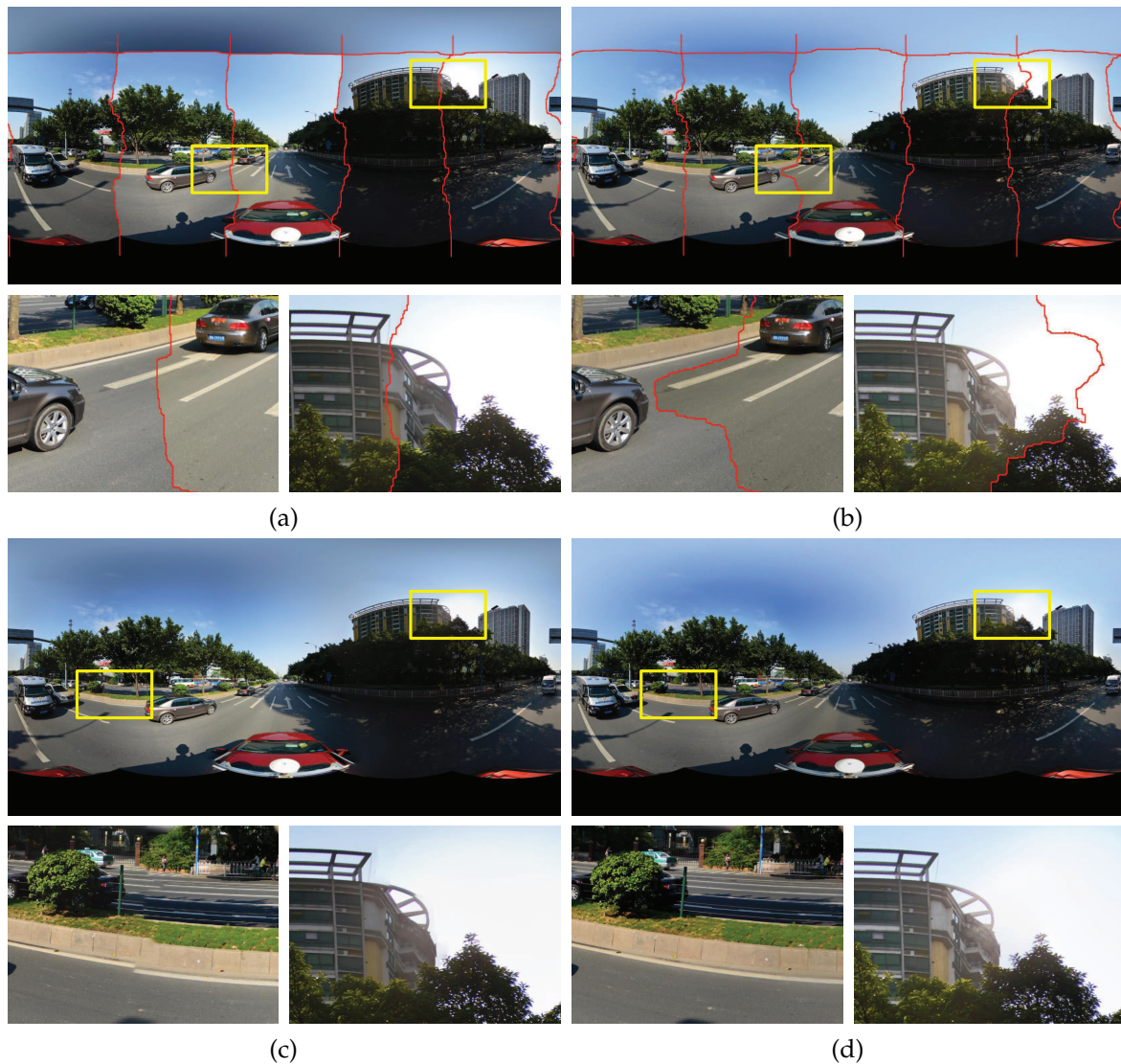


Figure 12. Visual comparison in the second group of six panoramic images: (a)-(b) the stitching results with the optimal seamlines when the our proposed color correction was used (b) or not (a); (c)-(d) the last panoramas generated by *Enblend* (c) and our proposed stitching system (d).

520 5.3 Image Stitching

521 To illustrate the effectiveness of our proposed framework for street-view panorama stitching,
 522 we presented the last panoramas stitched by different combination of optimal seamline detection
 523 (*S*), image warping (*W*), color correction (*C*) and image blending (*B*) algorithms in Figure 13. At
 524 first, Figure 13(a) shows the panorama generated by the optimal seamline detection algorithm
 525 presented by [19], from which we can find that there are many stitching artifacts caused by geometric
 526 misalignments and photometric inconsistencies in the last stitching image, especially obvious in
 527 the detailed local regions. For example, the white lanes on the road were broken due to the
 528 large geometric dislocations. In addition, there also exist large color differences along the optimal
 529 seamlines. Our proposed image warping and color correction algorithm can eliminate large geometric
 530 misalignments and photometric inconsistencies, as shown in Figures 13(b) and (c), respectively. The
 531 last blended panorama generated by our proposed system is shown in Figure 13(d) from which we
 532 can observe that the last stitched panoramic image is pleasant and high-quality, which can meet the
 533 application requirement of the street-view map.

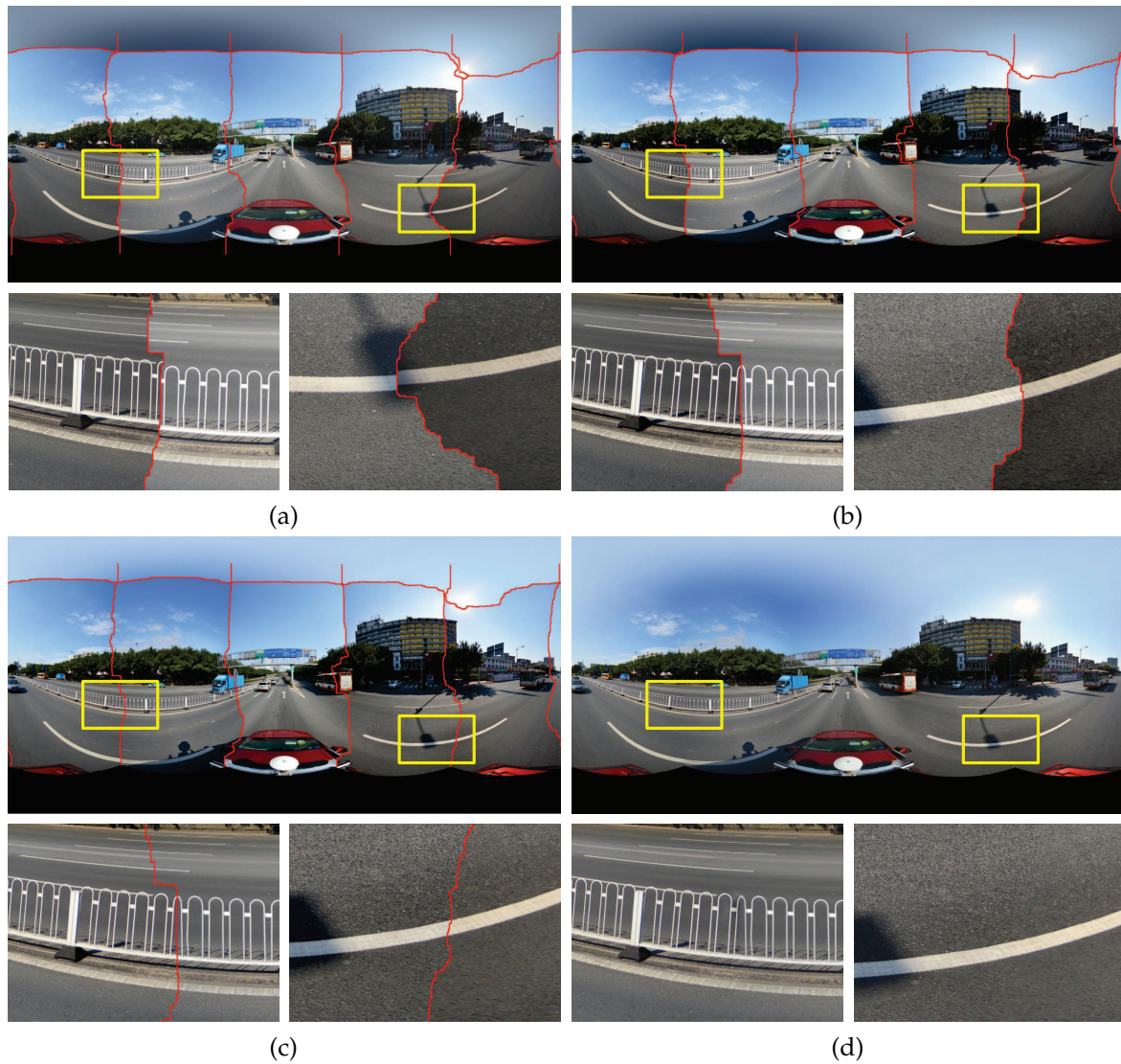


Figure 13. The stitching results with different combination of optimal seamline detection (S), image warping (W), color correction (C) and image blending (B) algorithms: (a) S (the result generated by [19]); (b) $W + S$; (c) $W + C + S$; (d) $W + C + S + B$. The computational times of (a)-(d) are 18.00s, 69.08s, 86.63s and 123.68s, respectively.

534 5.4 Comparative Results

535 At last, to prove that our approach is superior and can generate high-quality panoramas,
 536 we compared our proposed approach with the Xiong and Pulli's approach [42]. We used two
 537 representative groups of panoramic images for visual comparison. The color differences in the first
 538 group of images are relatively small but large in the second group. Because the Xiong and Pulli's
 539 approach has not eliminated the influence of large geometric misalignments between aligned images,
 540 so we used the warped images generated by our image warping algorithm as the input ones for
 541 comparing two approaches. In addition, their approach applied the Poisson blending algorithm
 542 to generate the last blended image, however, our approach used the Laplacian pyramid blending
 543 algorithm. To evaluate the last blended panoramas generated by two approaches fairer, we replaced
 544 the Poisson blending algorithm in the tested Xiong and Pulli's approach with the Laplacian pyramid
 545 blending algorithm.

546 Figure 14 shows the stitching results of the first group of images with relatively small color
547 differences. Figures 14(a) and (b) illustrate the stitching results just with the detected seamlines of the
548 Xiong and Pulli's approach and our approach without the use of color correction, respectively. From
549 these two figures, we can observe that the seamlines detected by our approach are better than those
550 detected by their approach. For example, the seamlines detected by their approach crossed the tall
551 building, but our approach avoided crossing it. Figures 14(c) and (d) illustrate the stitching results of
552 two approaches with the use of color correction, respectively, from which we observed that both of
553 two approaches can eliminate the small color differences effectively. Figures 14(e) and (f) show the
554 last blended panoramas generated by two approaches, respectively, from which we found that there is
555 some petty ghost on the top of the tallest building in the second enlarged region shown in Figure 14(e),
556 which disappeared in the panorama generated by our approach, as shown in Figure 14(f). This
557 is mainly because the horizontal seamline between bottom and top input images detected by the
558 Xiong and Pulli's approach is close to this building, as shown in Figure 14(c). In conclusion, if the
559 color differences between input images are small, both of two approaches can generate high-quality
560 panoramas.

561 Figure 15 shows the stitching results of the second group of images with very large color
562 differences. Figures 14(a) and (b) show the stitching results of the Xiong and Pulli's approach and our
563 approach without the use of color correction, respectively, from which we observed that our approach
564 also generated more high-quality seamlines than their approach. Figures 14(c) and (d) present the
565 stitching results of two approaches with the use of color correction, respectively. From the visual
566 comparison, we observed that our proposed color correction algorithm obviously outperformed than
567 the algorithm presented in [42], especially obvious in two locally enlarged regions. For example,
568 in the first enlarged region (from left to right), the detected seamline divides the building into two
569 parts, one comes from the top input image which is dark, and another comes from the bottom input
570 image which is relatively lighter. After color correction, the top image is also very dark in the result
571 generated by the Xiong and Pulli's approach and the color differences along the seamline are also
572 very large. In addition, due to that the top image is too dark, many detailed informations cannot
573 be pleasantly observed. But, in our result, the color of the top image is similar with the bottom one,
574 and more detailed informations of this region can be clearly observed. Figures 14(e) and (f) show the
575 last blended panoramas generated by two approaches, respectively. In the second enlarged region
576 of Figure 15(e), we found that there are some very obvious ghosts on the top of the building, which
577 disappeared in the panorama generated by our approach, as shown in Figure 15(f). In addition, in
578 Figure 15(e), the color of top sky regions almost is white, which is not pleasant. However, in the
579 last panorama generated by our approach, the color of those regions is slightly bluish, which is more
580 reasonable and pleasant, as shown in Figure 15(f). In conclusion, if the color differences between input
581 images are large, our approach can also generate high-quality panoramas, but the results generated
582 by the Xiong and Pulli's approach are not so good.

583 In the aspect of computational times of two approaches, the average times on two groups of
584 images are presented in Table 1, from which we can find that our approach is a litter bit more
585 time-consuming than their approach. This is mainly because their approach applied dynamic
586 programming to detect the optimal seamlines but we used graph cuts, which is more time-consuming
587 than dynamic programming. We also observed that the computation times of our proposed color
588 correction algorithm and their algorithm are 16.83s and 16.08s, respectively, which are almost the
589 same. But our color correction algorithm is more effective than their algorithm.

590 6 Conclusion

591 In this paper, we proposed a unified framework for street-view panorama stitching system which
592 is comprised of image warping, color correction, optimal seamline detection and image blending
593 for stitching or mosaicking a set of geometrically aligned street-view panoramic images with large

Table 1. The computational times of our proposed approach and the approach proposed in [42].

	Optimal Seamline Detection	Color Correction	Image Blending	#Total
Our Proposed Approach (s)	16.92	16.83	36.60	70.36
Xiong and Pulli's Approach (s)	13.77	16.08	36.72	66.5815

594 geometric misalignments and photometric inconsistencies into a visual-appealing and informative
 595 wide-angle composite image. The contributions in this paper are summarized as follows:

- 596 • We creatively proposed a novel image warping method based on the dense optical flows
 597 to greatly reduce the large geometric misalignment existed in the input images as much as
 598 possible. Experimental results have demonstrated the superiority of our proposed image
 599 warping method, which can efficiently and greatly eliminate the influence of the large geometric
 600 misalignment.
- 601 • We proposed a novel color correction and image blending method to further reduce the
 602 color differences between panoramic images based on extreme point matching of histograms
 603 of the overlapped image regions of two involved images via both probability density
 604 functions and cumulative distribution functions. Experimental results on representative
 605 street-view panoramic images have proved that our proposed color correction method is
 606 capable of eliminating the large color differences between adjacent images captured in different
 607 illumination conditions and/or different exposure settings, which obviously outperforms the
 608 open-source software *Enblend* and the approach proposed by [42].
- 609 • We proposed a unified framework for street-view panorama stitching system. Even though
 610 there are large geometrical misalignments and photometric inconsistencies in the input aligned
 611 images, our system can also generate pleasant and high-quality panoramas.

612 Nevertheless, the proposed system may be improved in the future in the following ways. First,
 613 when detecting the optimal seamlines, the superpixel segmentation can be introduced to greatly
 614 improve the optimization efficiency by decreasing the number of elements in graph cuts, and the
 615 scene understanding or parsing can also be applied in some particular image data. For example, the
 616 roads can be detected out for guiding the seamlines. Second, the whole image mosaicking method
 617 can be improved to handle more different types of images, not only street-view panoramic ones, but
 618 also aerial and oblique ones. At last, the parallel optimization strategy is expected to be developed to
 619 more efficiently generate the last panorama.

620 Acknowledgment

621 This work was partially supported by the National Natural Science Foundation of China (Project
 622 No. 41571436), the Hubei Province Science and Technology Support Program, China (Project No.
 623 2015BAA027), the National Natural Science Foundation of China (Project No. 41271431), and the
 624 Jiangsu Province Science and Technology Support Program, China (Project No. BE2014866).

625 Bibliography

- 626 1. Du, Q.; Raksuntorn, N.; Orduyilmaz, A.; Bruce, L.M. Automatic registration and mosaicking for airborne
 627 multispectral image sequences. *Photogrammetric Engineering & Remote Sensing* **2008**, *74*, 169–181.
- 628 2. Chon, J.; Kim, H.; Lin, C.S. Seam-line determination for image mosaicking: A technique minimizing the
 629 maximum local mismatch and the global cost. *ISPRS Journal of Photogrammetry and Remote Sensing* **2010**,
 630 *65*, 86–92.

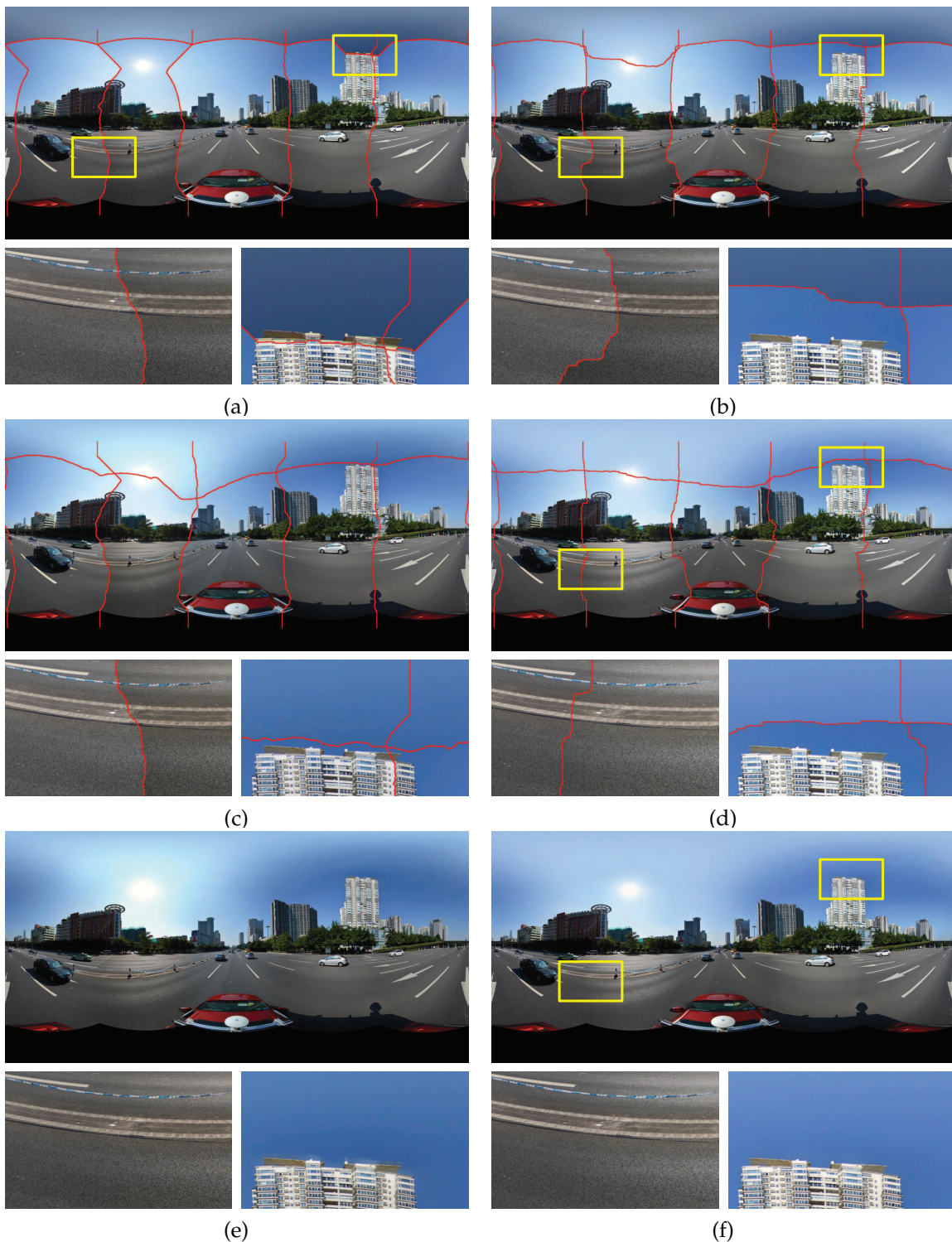


Figure 14. Visual comparison between our approach in the left column and the Xiong and Pulli's approach in the right column on the first group of images with relatively small color differences: (a)-(b) the results without the use of color correction; (c)-(d) the results with the use of color correction; (e)-(f) the last generated panoramas.

- 631 3. Wan, Y.; Wang, D.; Xiao, J.; Lai, X.; Xu, J. Automatic determination of seamlines for aerial image
 632 mosaicking based on vector roads alone. *ISPRS Journal of Photogrammetry and Remote Sensing* **2013**,
 633 76, 1–10.

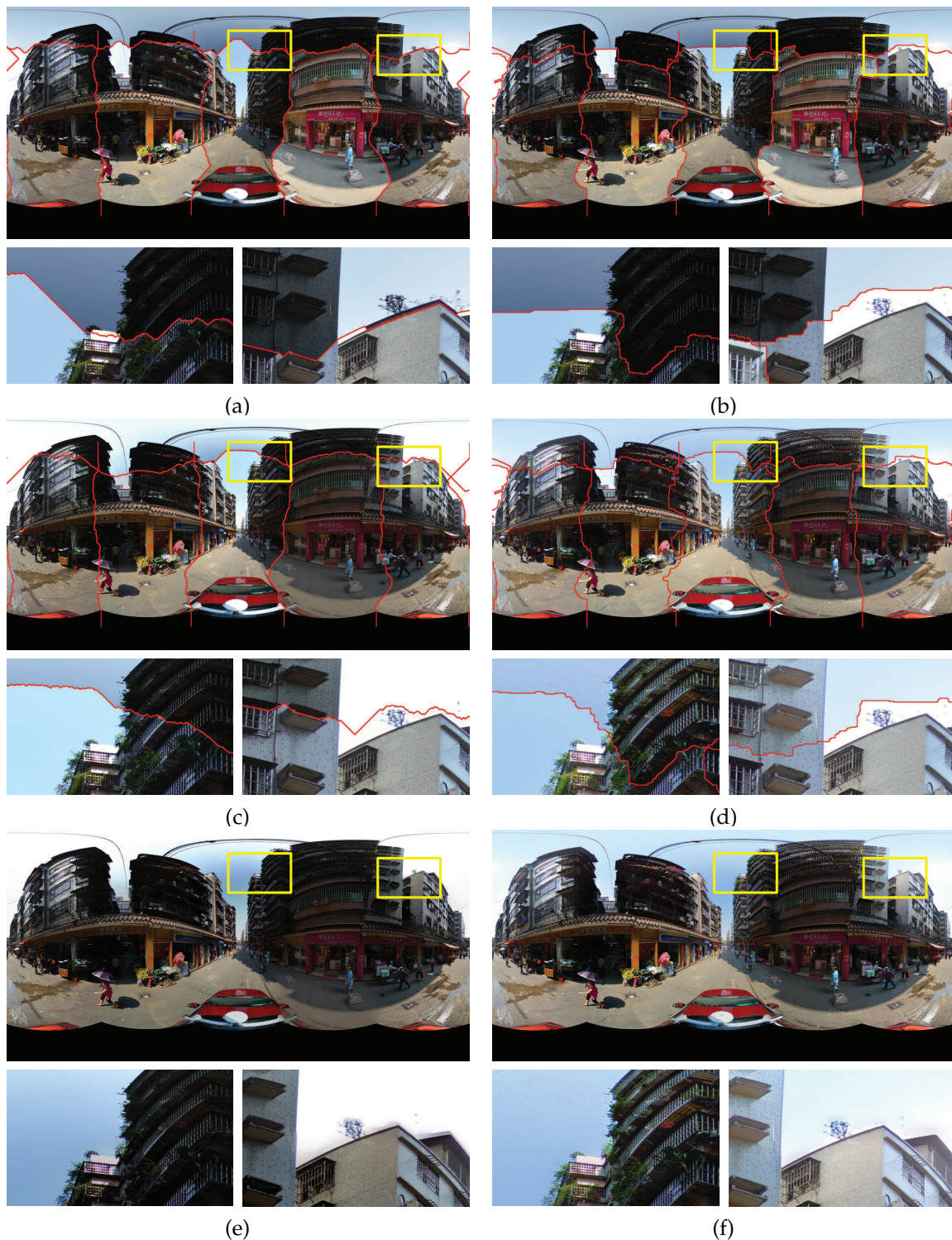


Figure 15. Visual comparison between our approach in the left column and the Xiong and Pulli's approach in the right column on the second group of images with large color differences: (a)-(b) the results without the use of color correction; (c)-(d) the results with the use of color correction; (e)-(f) the last generated panoramas.

- 634 4. Pan, J.; Zhou, Q.; Wang, M. Seamline Determination Based on Segmentation for Urban Image Mosaicking.
 635 *IEEE Transactions on Geoscience and Remote Sensing Letters* **2014**, *11*, 1335–1339.

- 636 5. Pang, S.; Sun, M.; Hu, X.; Zhang, Z. SGM-based seamline determination for urban orthophoto
637 mosaicking. *ISPRS Journal of Photogrammetry and Remote Sensing* **2016**, *112*, 1–12.
- 638 6. Kerschner, M. Seamline detection in colour orthoimage mosaicking by use of twin snakes. *ISPRS Journal*
639 *of Photogrammetry and Remote Sensing* **2001**, *56*, 53–64.
- 640 7. Soille, P. Morphological image compositing. *IEEE Transactions on Pattern Analysis and Machine Intelligence*
641 **2006**, *28*, 673–683.
- 642 8. Yang, Y.; Gao, Y.; Li, H.; Han, Y. An algorithm for remote sensing image mosaic based on valid area.
643 International Symposium on Image and Data Fusion (ISIDF), 2011.
- 644 9. Li, X.; Hui, N.; Shen, H.; Fu, Y.; Zhang, L. A robust mosaicking procedure for high spatial resolution
645 remote sensing images. *ISPRS Journal of Photogrammetry and Remote Sensing* **2015**, *109*, 108–125.
- 646 10. Agarwala, A.; Dontcheva, M.; Agrawala, M.; Drucker, S.; Colburn, A.; Curless, B.; Salesin, D.; Cohen, M.
647 Interactive Digital Photomontage. *ACM Transactions on Graphics (TOG)* **2004**, *23*, 294–302.
- 648 11. Szeliski, R. Image alignment and stitching: A tutorial. *Foundations and Trends® in Computer Graphics and*
649 *Vision* **2006**, *2*, 1–104.
- 650 12. Brown, M.; Lowe, D.G. Automatic panoramic image stitching using invariant features. *International*
651 *Journal of Computer Vision* **2007**, *74*, 59–73.
- 652 13. Gracias, N.; Mahoor, M.; Negahdaripour, S.; Gleason, A. Fast image blending using watersheds and
653 graph cuts. *Image and Vision Computing* **2009**, *27*, 597–607.
- 654 14. Prados, R.; Garcia, R.; Gracias, N.; Escartin, J.; Neumann, L. A novel blending technique for underwater
655 gigamosaicing. *IEEE Journal of Oceanic Engineering* **2012**, *37*, 626–644.
- 656 15. Philip, S.; Summa, B.; Tierny, J.; Bremer, P.T.; Pascucci, V. Distributed Seams for Gigapixel Panoramas.
657 *IEEE Transactions on Visualization and Computer Graphics* **2015**, *21*, 350–362.
- 658 16. Kwatra, V.; Schödl, A.; Essa, I.; Turk, G.; Bobick, A. Graphcut Textures Image and Video Synthesis Using
659 Graph Cuts. *ACM Transactions on Graphics (TOG)* **2003**, *22*, 277–286.
- 660 17. Yu, L.; Holden, E.J.; Dentith, M.C.; Zhang, H. Towards the automatic selection of optimal seam line
661 locations when merging optical remote-sensing images. *International Journal of Remote Sensing* **2012**,
662 *33*, 1000–1014.
- 663 18. Mills, S.; McLeod, P. Global seamline networks for orthomosaic generation via local search. *ISPRS Journal*
664 *of Photogrammetry and Remote Sensing* **2013**, *75*, 101–111.
- 665 19. Li, L.; Yao, J.; Lu, X.; Tu, J.; Shan, J. Optimal seamline detection for multiple image mosaicking via graph
666 cuts. *ISPRS Journal of Photogrammetry and Remote Sensing* **2016**, *113*, 1–16.
- 667 20. Kass, M.; Witkin, A.; Terzopoulos, D. Snakes: active contour models. *International Journal of Computer*
668 *Vision* **1988**, *1*, 321–331.
- 669 21. Dijkstra, E.W. A note on two problems in connexion with graphs. *Numerische Mathematik* **1959**, *1*, 269–271.
- 670 22. Bellman, R. *Dynamic Programming*; Princeton University Press, Princeton, NJ, 1957.
- 671 23. Boykov, Y.; Veksler, O.; Zabih, R. Fast approximate energy minimization via graph cuts. *IEEE Transactions*
672 *on Pattern Analysis and Machine Intelligence* **2001**, *23*, 1222–1239.
- 673 24. Glasbey, C.A.; Mardia, K.V. A review of image-warping methods. *Journal of Applied Statistics* **1998**,
674 *25*, 155–171.
- 675 25. Lee, S.Y.; Chwa, K.Y.; Hahn, J.K.; Shin, S.Y. Image morphing using deformation techniques. *Journal of*
676 *Visualization and Computer Animation* **1996**, *7*, 3–23.
- 677 26. Liao, J.; Lima, R.S.; Nehab, D.; Hoppe, H.; Sander, P.V.; Yu, J. Automating image morphing using
678 structural similarity on a halfway domain. *ACM Transactions on Graphics (TOG)* **2014**, *33*, 1–12.
- 679 27. Liu, F.; Gleicher, M. Automatic image retargeting with fisheye-view warping. *ACM Symposium on User*
680 *Interface Software and Technology*, 2005, pp. 153–162.
- 681 28. Lin, S.S.; Yeh, I.C.; Lin, C.H.; Lee, T.Y. Patch-based image warping for content-aware retargeting. *IEEE*
682 *Transactions on Multimedia* **2013**, *15*, 359–368.
- 683 29. Zaragoza, J.; Chin, T.J.; Brown, M.; Suter, D. As-projective-as-possible image stitching with moving DLT.
684 *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2013, pp. 2339–2346.
- 685 30. Lin, C.C.; Pankanti, S.U.; Ramamurthy, K.N.; Aravkin, A.Y. Adaptive as-natural-as-possible image
686 stitching. *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2015, pp. 1155–1163.
- 687 31. Bookstein, F.L. Principal warps: Thin-plate splines and the decomposition of deformations. *IEEE*
688 *Transactions on Pattern Analysis and Machine Intelligence* **1989**, *11*, 567–585.

- 689 32. Alexa, M.; Cohen-Or, D.; Levin, D. As-Rigid-As-Possible Shape Interpolation. International Conference
690 on Computer Graphics and Interactive Techniques Conference (SIGGRAPH), 2000, pp. 157–164.
- 691 33. Igarashi, T.; Moscovich, T.; Hughes, J.F. As-rigid-as-possible shape manipulation. *ACM transactions on*
692 *Graphics (TOG)* **2005**, *24*, 1134–1141.
- 693 34. Schaefer, S.; McPhail, T.; Warren, J. Image deformation using moving least squares. *ACM transactions on*
694 *graphics (TOG)*, 2006, Vol. 25, pp. 533–540.
- 695 35. Levin, D. The approximation power of moving least-squares. *Mathematics of Computation of the American*
696 *Mathematical Society* **1998**, *67*, 1517–1531.
- 697 36. Chen, T.L.; Geman, S. Image warping using radial basis functions. *Journal of Applied Statistics* **2014**,
698 *41*, 242–258.
- 699 37. Lee, S.; Wolberg, G.; Shin, S.Y. Scattered data interpolation with multilevel B-splines. *IEEE Transactions*
700 *on Visualization and Computer Graphics* **1997**, *3*, 228–244.
- 701 38. Yao, J. Modeling and Rendering from Multiple Views. PhD thesis, The Chinese University of Hong Kong,
702 2006.
- 703 39. Yao, J.; Cham, W.K. 3D modeling and rendering from multiple wide-baseline images by match
704 propagation. *Signal Processing: Image Communication* **2006**, *21*, 506–518.
- 705 40. Xu, W.; Mulligan, J. Performance evaluation of color correction approaches for automatic multi-view
706 image and video stitching. *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2010,
707 pp. 263–270.
- 708 41. Tian, G.Y.; Gledhill, D.; Taylor, D.; Clarke, D. Colour correction for panoramic imaging. *International*
709 *Conference on Information Visualisation*, 2002, Vol. 215, pp. 483–488.
- 710 42. Xiong, Y.; Pulli, K. Fast panorama stitching for high-quality panoramic images on mobile phones. *IEEE*
711 *Transactions on Consumer Electronics* **2010**, *56*, 298–306.
- 712 43. Hwang, Y.; Lee, J.Y.; Kweon, I.S.; Kim, S.J. Color transfer using probabilistic moving least squares. *IEEE*
713 *Conference on Computer Vision and Pattern Recognition (CVPR)*, 2014, pp. 3342–3349.
- 714 44. Yamamoto, K.; Oi, R. Color correction for multi-view video using energy minimization of view networks.
715 *International Journal of Automation and Computing* **2008**, *5*, 234–245.
- 716 45. Lowe, D. Distinctive Image Features from Scale-Invariant Keypoints. *International Journal of Computer*
717 *Vision* **2004**, *60*, 91–110.
- 718 46. Fecker, U.; Barkowsky, M.; Kaup, A. Histogram-based prefiltering for luminance and chrominance
719 compensation of multiview video. *IEEE Transactions on Circuits and Systems for Video Technology* **2008**,
720 *18*, 1258–1267.
- 721 47. Uyttendaele, M.; Eden, A.; Skeliski, R. Eliminating ghosting and exposure artifacts in image mosaics.
722 *IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR)*, 2001, Vol. 2,
723 pp. II–509.
- 724 48. Porter, T.; Duff, T. Compositing Digital Images. *ACM SIGGRAPH Computer Graphics* **1984**, *18*, 253–259.
- 725 49. Burt, P.J.; Adelson, E.H. A multiresolution spline with application to image mosaics. *ACM Transactions*
726 *on Graphics (TOG)* **1983**, *2*, 217–236.
- 727 50. Pérez, P.; Gangnet, M.; Blake, A. Poisson image editing. *ACM Transactions on Graphics (TOG)* **2003**,
728 *22*, 313–318.
- 729 51. Levin, A.; Zomet, A.; Peleg, S.; Weiss, Y. Seamless image stitching in the gradient domain. *European*
730 *Conference on Computer Vision (ECCV)*, 2004.
- 731 52. Yao, J.; Cham, W.K. Robust multi-view feature matching from multiple unordered views. *Pattern*
732 *Recognition* **2007**, *40*, 3081–3099.
- 733 53. Bay, H.; Tuytelaars, T.; Gool, L.V. SURF: Speeded Up Robust Features. *Computer Vision & Image*
734 *Understanding* **2006**, *110*, 404–417.
- 735 54. HaCohen, Y.; Shechtman, E.; Goldman, D.B.; Lischinski, D. Optimizing color consistency in photo
736 collections. *ACM Transactions on Graphics (TOG)* **2013**, *32*, 38:1–38:10.